

# GENERALIZED NET MODEL OF ALGORITHM FOR NON-CONFLICT SWITCH IN PACKET COMMUNICATION NODE \*

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## **1. Introduction.**

In time-multiplex communication systems, crossbar packet switches route traffic from the input to output where a message packet is transmitted from the source to the destination. The randomly incoming traffic must be controlled and scheduled to eliminate conflict at the crossbar switch where the conflict is that two or more users may simultaneously access to a single output. The goal of the traffic-scheduling for the time-multiplex crossbar switches is not only to maximize the throughput of packet through a crossbar switch but also to minimize packet blocking probability and packet waiting time [1].

The researchers presented the technique utilized in the algorithm is a systematic method of finding distinct representatives from the row sets of a traffic matrix, algorithm based on a cellular automaton and neural network [1,2]. We consider that the Generalized nets (GN) [3,4] may be used for modelling of such tasks because of its possibilities to model as the structure of the investigated object, as the dynamics of the flowing in it processes. The GN are contemporary development, suggesting detail reflection of the structure and time relation in parallel processes.

In this paper we shall use GN apparatus for construction of model of algorithm for non-conflict switched, allowing zero blocking probability.

## **2. Algorithm for non-conflict switched.**

A request for packet transmission through an  $n \times n$  crossbar is described by an  $n \times n$  traffic matrix  $T$ . In the traffic matrix  $T$ , each element  $t_{ij}$  ( $t_{ij} \in [0,1]$ ) represents a request of packets from input  $i$  to output  $j$ . For example,  $t_{ij}=0$  means that there is no packet to be transmitted on the  $j$ th output

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line from the  $i$ th input line.  $t_{ij}=1$  means that at least one packet on the  $i$ th input line should be transmitted on the  $j$ th output line of the crossbar [2].

Conflict situation is created when at any row of the traffic matrix the number of ones is bigger than one. This is corresponding to case when one source announces connection with more than one receiver. Existence of more than one (1) at any column of matrix  $T$  is also showing that conflict situation is available and means, that more than one source is announced connection to the same receiver [5]. Avoiding of the conflicts is directly related to the efficiency of the communication node.

The presented algorithm calculates a set of matrices  $R$ , which has a only one element consist 1 (if exist) in each row and column. This set determines a non-conflict schedule to transmit a request at switch.

The sense of the suggested algorithm is the following : we copy matrix  $T$  in intermediate matrix  $M$ . That matrix  $M$  is checked sequentially along the rows if one (1) is available. By the first middle one (1) we write in this cell of the matrix  $T$  zero (0), and in matrix  $M$  under this cell – in this column – zero (0). Value of this cell (1) is written in the same cell of new matrix  $R$ , which we call matrix of allowed non-conflict switches.

After that we go to the next row of the matrix  $M$  until we check all rows. After checking the last row of the matrix  $M$  is formed matrix  $R$ , which contains no conflicts and  $R$  is delivered for control of the contains transmission. The matrix  $T$  already no sented for transmission requests.

The process is iterative. After the first formed non-conflict matrix  $R$  we copy already changed matrix  $T$  in intermediate matrix  $M$  and repeat the searching. The algorithm ends its action when in matrix  $T$  no one (1) is available i.e. all the requests are satisfied.

### **3. GN-model of the algorithm.**

Our task is to construct a model of the algorithm in type of GN, and the purpose is the so obtained GN to be easy to scale (to allow parallelism).

The offered decision in GN type is showed on the fig.1.

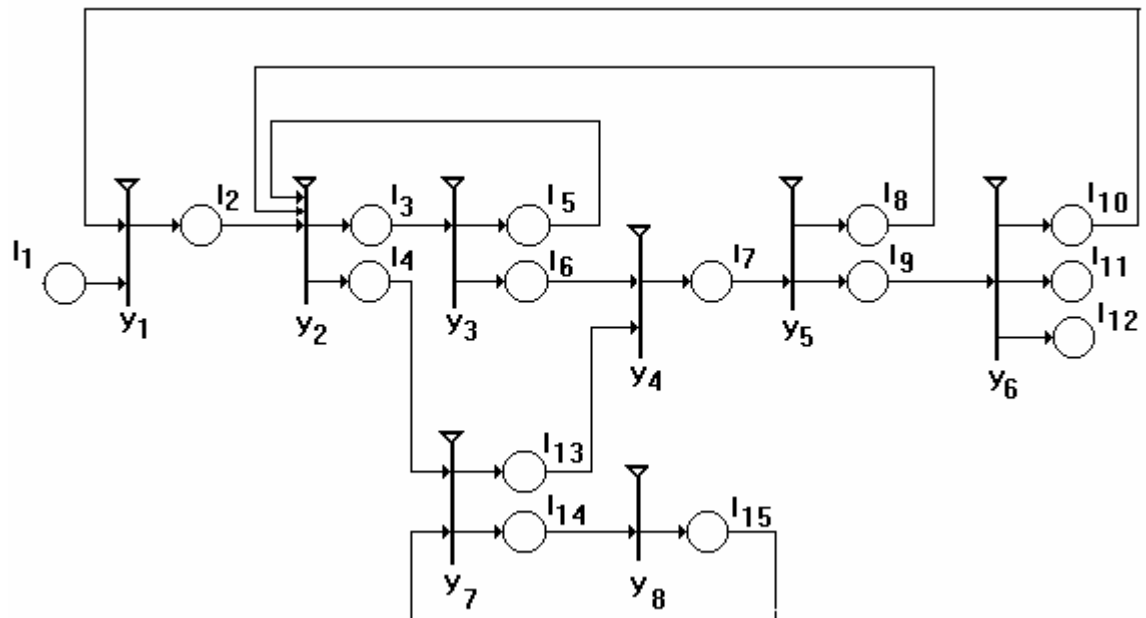
The tokens in the GN-model presented the matrix and variables. The token has nine parameters : <size>, <traffic matrix>, <iteration>, <intermediate matrix>, <non-conflict matrix>, <number of row>, <number of column>, < number of intermediate cell>, <number of non-conflict request>.

The parameter  $\langle \text{size} \rangle$  has size  $n \hat{I} N$  ( $n \times n$ ) of matrix T, M and R. The parameter  $\langle \text{traffic matrix} \rangle$  showed the traffic matrix T. The parameter  $\langle \text{iteration} \rangle$  showed the number of iterations. The parameter  $\langle \text{intermediate matrix} \rangle$  showed the intermediate matrix M. The parameter  $\langle \text{non-conflict matrix} \rangle$  showed the switched matrix  $R^k: R^1, R^2, \dots, R^k, k \hat{I} [1, n]$ . The parameter  $\langle \text{number of row} \rangle$  showed the number of row of matrix :  $i \hat{I} [1, n]$ . The parameter  $\langle \text{number of column} \rangle$  showed the number of column of matrix :  $j \hat{I} [1, n]$ . The parameter  $\langle \text{number of intermediate cell} \rangle$  showed the number of intermediate cell under the  $t_{ij}=1$ . The parameter  $\langle \text{number of non-conflict request} \rangle$  showed the number of elements  $t_{ij}=1$  in current iteration.

The token  $\alpha$  come into place  $l_1$  with initial characteristic “ $\langle \text{size} \rangle = n, \langle \text{traffic matrix} \rangle := T, \langle \text{iteration} \rangle = 1 (k=1)$ ”

The concrete descriptions of places is :

- |                                    |  |
|------------------------------------|--|
| $l_1$ - start;                     | $l_2$ - initial parameters;                      |
| $l_3$ - no request ( $M_{ij}=0$ ); | $l_4$ - request for transmission ( $M_{ij}=1$ ); |
| $l_5$ - the row is not eluded;     | $l_6$ - the row is eluded ( $j > n$ );           |
| $l_7$ - to new row;                | $l_8$ - the M is not eluded;                     |
| $l_9$ - the M is eluded;           | $l_{10}$ - to new iteration;                     |



- |  |                                      |
|--|--------------------------------------|
| $l_{11}$ - the $R^k$ is ready;               | $l_{12}$ - stop;                     |
| $l_{13}$ - the column is eluded ( $l > n$ ); | $l_{14}$ - the column is not eluded; |
| $l_{15}$ - to new cell.                      |                                      |

Fig.1. GN-model of algorithm

The formal description is:

$$y_1 = \langle \{l_1, l_{10}\}, \{l_2\}, r_1, v(l_1, l_{10}) \rangle,$$

where

$$r_1 = \begin{array}{c|c} & l_2 \\ \hline l_1 & \text{true} \\ l_{10} & \text{true} \end{array}$$

The characteristic functions are :  $\Phi_2 = \langle \langle \text{intermediate matrix} \rangle := \langle \text{traffic matrix} \rangle (M := T), \langle \text{non-conflict matrix} \rangle = 0 (R^k := 0), \langle \text{number of row} \rangle = 1 (i := 1), \langle \text{number of column} \rangle = 1 (j := 1), \langle \text{number of non-conflict request} \rangle = 0 (r = 0) \rangle$  ”

$$r_2 = \begin{array}{c|cc} & l_3 & l_4 \\ \hline l_2 & \neg W_1 & W_1 \\ l_5 & \neg W_1 & W_1 \\ l_8 & \neg W_1 & W_1 \end{array}$$

$$y_2 = \langle \{l_2, l_5, l_8\}, \{l_3, l_4\}, r_2, v(l_2, l_5, l_8) \rangle,$$

where

The predicate  $W_1$  has the following forms:  $W_1 = \langle M_{ij} = 1 \rangle$  ;

The characteristic functions are :  $\Phi_3 = \langle \langle \text{number of column} \rangle := \langle \text{number of column} \rangle + 1 (j :=$

$$r_3 = \begin{array}{c|cc} & l_5 & l_6 \\ \hline l_3 & \neg W_2 & W_2 \end{array}$$

$j+1) \rangle$  ;  $\Phi_4 = \langle \langle T_{ij} \rangle := 0, \langle R^k_{ij} \rangle := 1, \langle \text{number of intermediate cell} \rangle := \langle \text{number of row} \rangle + 1 (l := i+1), \langle \text{number of non-conflict request} \rangle := \langle \text{number of non-conflict request} \rangle + 1 (r := r+1) \rangle$ ”.

$$y_3 = \langle \{l_3\}, \{l_5, l_6\}, r_3, v(l_3) \rangle,$$

where

The predicate  $W_2$  has the following forms:  $W_2 = \langle j > n \rangle$  .

The characteristic functions are “\*”:

$$y_4 = \langle \{l_6, l_{13}\}, \{l_7\}, r_4, v(l_6, l_7) \rangle,$$

$$r_4 = \begin{array}{c|c} & l_7 \\ \hline l_6 & \text{true} \\ l_{13} & \text{true} \end{array}$$

where

The characteristic functions are : $\Phi_7 = \langle \text{number of row} \rangle = \langle \text{number of row} \rangle + 1$  ( $i = i + 1$ )” .

$y_5 = \langle \{ l_7 \}, \{ l_8, l_9 \}, r_5, v(l_7) \rangle$  ,

$$r_5 = \begin{array}{c|cc} & l_8 & l_9 \\ \hline l_7 & \neg W_3 & W_3 \end{array}$$

where

The predicate  $W_3$  have the following forms:  $W_3 = \langle i \rangle > n$  “ .

The characteristic functions are : $\Phi_8 = \langle \text{number of column} \rangle = 1$  ( $j := 1$ )” ,  $\Phi_9 = \langle \text{“*”} \rangle$ .

$$r_6 = \begin{array}{c|ccc} & l_{10} & l_{11} & l_{12} \\ \hline l_9 & \neg W_4 & \text{true} & W_4 \end{array}$$

$y_6 = \langle \{ l_9 \}, \{ l_{10}, l_{11}, l_{12} \}, r_6, v(l_9) \rangle$  ,

where

The predicate  $W_4$  have the following forms:  $W_4 = \langle r \rangle = 0$  “ .

$$r_7 = \begin{array}{c|cc} & l_{13} & l_{14} \\ \hline l_4 & W_5 & \neg W_5 \\ l_{15} & W_5 & \neg W_5 \end{array}$$

The characteristic functions are :  $\Phi_{10} = \langle \text{iteration} \rangle = \langle \text{iteration} \rangle + 1$  ( $k := k + 1$ )” ,  $\Phi_{11} = \langle \text{“<R^k> to swich”} \rangle$ , .  $\Phi_{12} = \langle \text{“*”} \rangle$ .

$y_7 = \langle \{ l_4, l_{15} \}, \{ l_{13}, l_{14} \}, r_7, v(l_4, l_{15}) \rangle$  ,

where

$$r_8 = \begin{array}{c|c} & l_{15} \\ \hline l_{14} & \text{true} \end{array}$$

The predicate  $W_5$  have the following forms:  $W_5 = \langle l \rangle > n$  “ .

The characteristic functions are :  $\Phi_{13} = \langle \text{“*”} \rangle$  ,  $\Phi_{14} = \langle \text{“<M}_{ij} \rangle = 0$ ”.

$y_8 = \langle \{ l_{14} \}, \{ l_{15} \}, r_8, v(l_{14}) \rangle$  ,

where

The characteristic functions are :  $\Phi_{15} = \langle \text{number of intermediate cell} \rangle := \langle \text{number of intermediate cell} \rangle + 1$  ( $l := l + 1$ ).

Capacity of all arcs are equal to one. Capacity of all places is also one, except of place  $l_{11}$ , which has capacity  $n$ . Priorities of places are equivalent, priorities of transitions are equivalent – i.e. priorities are not necessarily. The GN has no local and global temporal components.

The chosen way of searching of the matrix  $M$  introduces priorities in the service of requests. The requests, corresponding to the element  $t_{1,1}$  will be serviced first, and  $t_{nn}$  – last. The priorities of service may be change through transposition of row and columns of the matrix  $T$ .

#### **4. Conclusion.**

The specified algorithm is with sequent action – in a single time interval fires only one transition, but the task allows parallelism. By division of the matrix  $T$  into 4 submatrix (2x2) two computing devices can work following the such described algorithm parallelly. If we have 9 submatrix (3x3), 3 parallel devices can be used i.e. to  $n$  parallel devices.

A task for investigation is to determine the best and worst time for satisfaction of the request. This is the object of our current investigations therefore the so constructed GN model has a potential for investigation.

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