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Research on intuitionistic fuzzy implications. Part 2

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Abstract: Continuing the research from [2], here we give the list of the axioms that are satisfied by the intuitionistic fuzzy implications, introduced in Part 1 of the present research. Given the large number of implications that have already been defined and the naturally arising question about their comparability and usability, we discuss the criteria of usability of implications and outline 44 ones that satisfy at least 28 from the discussed 38 axioms, that is about 1/4 of all implications that satisfy at least about 3/4 of all axioms. Finally, we show the relationships between each pair of implications in the form of a graph.

Keywords: Intuitionistic fuzzy implication, Intuitionistic fuzzy pair, Intuitionistic fuzzy set, Logic axiom.

2020 Mathematics Subject Classification: 03E72.

1 Introduction

In Part 1 of the present research [2], giving short remarks on the results related to the intuitionistic fuzzy implications, for the first time in fuzzy sets theory, we introduced the relations between separate implications.

All necessary definitions and notations are given in Part 1, but below, we will repeat a part of them, wherever this is appropriate.

2 Main results

First, we give the list of logic axioms for which all presently defined intuitionistic fuzzy implications will be tested. These axioms (see [4]) are intuitionistic fuzzy adaptations of:

- the axioms of Klir and Yuan [5], except for Axiom $A9: \rightarrow$ is a continuous function,
- modifications of Klir and Yuan's axioms A3, A4, A5, A7 (two forms) and A8 (see [4]),
- the axioms of intuitionistic logic [6],
- the axioms of Kolmogorov (see, e.g. [7]),
- relations between logical constants (from A31 to A38).

Let

$$O^* = \langle 0, 1 \rangle, \qquad U^* = \langle 0, 0 \rangle, \qquad E^* = \langle 1, 0 \rangle.$$

We use the following axioms:

A1
$$(\forall x, y)((x \le y) \to (\forall z)(x \to z \ge y \to z)),$$

$$A2 \ (\forall x, y)((x \le y) \to (\forall z)(z \to x \le z \to y)),$$

A3
$$(\forall y)(O^* \rightarrow y = E^*)$$
,

$$A4 \ (\forall y)(O^* \to y \text{ is an IFT}),$$

$$A5 \ (\forall y)(E^* \rightarrow y = y),$$

$$A6 \ (\forall y)(E^* \to y < y),$$

A7
$$(\forall x)(x \to x = E^*)$$
,

A8
$$(\forall x)(x \to x \text{ is an IFT})$$
,

$$A9 \ (\forall x, y, z)(x \to (y \to z) = y \to (x \to z)),$$

A10
$$(\forall x, y)(x \rightarrow y = 1 \text{ if and only if } x \leq y)$$
,

A11
$$(\forall x, y)((x < y) \rightarrow (x \rightarrow y = E^*)),$$

$$A12 \ (\forall x, y)(x \to y = \neg y \to \neg x),$$

A13
$$(\forall x, y)(x \rightarrow y = \neg \neg (\neg y \rightarrow \neg x)),$$

$$A14 \ A \rightarrow (B \rightarrow A),$$

$$A15 \ A \rightarrow (B \rightarrow (A \land B)),$$

A16
$$(A \rightarrow (B \rightarrow C)) \rightarrow (B \rightarrow (A \rightarrow C)),$$

A17 $(A \rightarrow (B \rightarrow C)) \rightarrow ((A \rightarrow B) \rightarrow (A \rightarrow C)),$
A18 $A \rightarrow \neg \neg A,$
A19 $\neg (A \land \neg A),$
A20 $(\neg A \lor B) \rightarrow (A \rightarrow B),$
A21 $\neg (A \lor B) \rightarrow (\neg A \land \neg B),$
A22 $(\neg A \land \neg B) \rightarrow \neg (A \lor B),$
A23 $(\neg A \lor \neg B) \rightarrow \neg (A \land B),$
A24 $(A \rightarrow B) \rightarrow (\neg B \rightarrow \neg A),$
A25 $(A \rightarrow \neg B) \rightarrow (B \rightarrow \neg A),$
A26 $\neg \neg \neg A \rightarrow \neg A,$
A27 $\neg A \rightarrow \neg \neg \neg A,$
A28 $\neg \neg (A \rightarrow B) \rightarrow (A \rightarrow \neg B),$
A29 $(C \rightarrow A) \rightarrow ((C \rightarrow (A \rightarrow B)) \rightarrow (C \rightarrow B)).$
A30 $(A \rightarrow (A \rightarrow B)) \rightarrow (A \rightarrow B)),$
A31 $(B \rightarrow C) \rightarrow ((A \rightarrow B) \rightarrow (A \rightarrow C)),$
A32 $(A \rightarrow B) \rightarrow ((A \rightarrow \neg B) \rightarrow \neg A),$
A33 $O^* \rightarrow O^*,$
A34 $O^* \rightarrow U^*,$
A35 $O^* \rightarrow E^*,$
A36 $E^* \rightarrow O^*,$
A37 $E^* \rightarrow U^*,$
A38 $E^* \rightarrow E^*.$

The full list of 182 implications that will be a subject of investigation is given in Part 1 of the present research, [2]. To analyse their satisfiability of the 38 axioms listed above, we use the software, described in [1], and the results are given in Table 1, where "+" and "-" denote whether the respective axiom has been satisfied by the respective implication, or not.

Remark. In the course of the present research, the authors discovered the following pairs (and one triple) of coinciding implications:

The difference of some of these implications was determined to be a result of their different lexicographic records, or as a result of misprinted numeration of implications at the moment of publication. The authors propose that in future only the respective first implication from the pair (triple) be used and identified, i.e., \rightarrow_{16} instead of \rightarrow_{181} , \rightarrow_{40} instead of \rightarrow_{173} , and so forth.

Table 1. Relationships between logic axioms and IF implications

	\rightarrow_1	\rightarrow_2	\rightarrow_3	\rightarrow_4	\rightarrow_5	\rightarrow_6	\rightarrow_7	\rightarrow_8	\rightarrow_9	\rightarrow_{10}	\rightarrow_{11}	\rightarrow_{12}	\rightarrow_{13}
1	_	+	+	+	+	_	_	+	_	_	+	+	+
2	+	+	+	+	+	+	_	+	+	+	+	+	+
3	+	+	+	+	+	+	_	+	+	+	+	+	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	+	_	+	+	+	+	+	_	+	+	+	_	+
6	+	+	+	+	+	+	+	+	+	+	+	+	+
7	_	+	+	_	_	_	_	+	_	_	+	_	_
8	+	+	+	+	+	+	+	+	+	_	+	_	+
9	_	_	+	+	+	_	_	_	_	_	+	+	+
10	_	_	_	_	_	_	_	_	_	_	_	_	_
11	_	+	+	_	_	_	_	+	_	_	+	_	_
12	_	_	_	+	+	_	+	_	_	_	_	_	+
13	_	_	_	+	+	_	+	_	_	_	_	_	+
14	+	_	+	+	+	+	+	_	+	_	+	_	+
15	+	_	+	+	+	+	_	_	_	_	+	_	+
16	+	_	+	+	+	+	_	_	+	_	+	+	+
17	+	+	+	+	+	_	_	_	+	_	+	+	+
18	+	+	+	+	+	+	+	+	+	_	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	_	+	+	+	+	_	_	+	_	+	_	+
21	+	+	+	+	+	+	+	+	+		+	+	+
22	+	+	+	+	+	+	+	+	+	_	+	+	+
23	+	+	+	+	+	+	+	+	+	_	+	+	
24	+	+	+	+	+	+	+	+	+	_	+	+	+
25	+	+	+	+	+	+	+	+	+		+	+	+
_26	+	+	+	+	+	+	+	+	+	_	+	+	+
27	+	+	+	+	+	+	+	+	+	_	+	+	+
_28	+	+	+	+	+	+	+	+	+		+	+	
29	+	+	+	+	+	_	_	_	+	_	+	+	+
30	+	+	+	+	+	+	+	+	+		+	+	+
31	+	+	+	+	+	_	_	_	+	_	+	+	+
32	+	+	+	+	+	_	+	+	+	_	+	+	
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	
37	+	+	+	+	+	+	+	+	+	+	+	_	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

	\rightarrow_{14}	\rightarrow_{15}	\rightarrow_{16}	\rightarrow_{17}	\rightarrow_{18}	\rightarrow_{19}	\rightarrow_{20}	\rightarrow_{21}	\rightarrow_{22}	\rightarrow_{23}	\rightarrow_{24}	\rightarrow_{25}	\rightarrow_{26}
1	+	+	+		+	+	+		+	+	+	+	+
2	+	+	+	+	+	+	+	_	+	+	+	+	+
3	+	+	+	+	+	+	+	+	+	+	+	+	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	+	_	+	+	+	+	_	_	_	_	_	_	+
6	+	+	+	+	+	+	_	_	_	_	+	+	+
7	+	+	_	_	_	_	+	_	_	+	+	_	_
8	+	+	_	+	+	_	+	+	+	+	+	_	_
9	+	_	+	+	+	+	+	_	+	+	_	+	+
10	+	+	_	_	_	_	_	_	_	_	+	_	_
11	+	+	_	_	_	_	+	_	_	+	+	_	
12	_	_	_	_	_	_	+	_	+	+	_	_	
13	_	_	_	_	_	_	+	_	+	+	_	_	_
14	+	_	_	+	+	_	+	+	+	+	_	_	_
15	+	_	_	+	+	_	+	+	+	+	_	_	_
16	+	_	_	+	+	_	+	_	+	+	_	+	_
17	+	_	_	+	+	_	+	+	+	+	+	+	_
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	_	_	+	+	_	+	+	+	+	_	_	_
21	+	+	+	+	+	+	+	+	+	+	+	+	+
22	+	+	+	+	+	+	+	+	+	+	+	+	+
23	+	+	+	+	+	+	+	+	+	+	+	+	+
24	+	+	+	+	+	+	+	+	+	+	+	+	+
25	+	+	+	+	+	+	+		+	+	+	+	+
26	+	+	+	+	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28	+	+	+	+	+	+	+	+	+	+	+	+	+
29	+	_	_	+	+	_	+	+	+	+	+	+	
30	+	+	_	+	+	_	+	+	+	+	+	+	
31	+	_	_	+	+	_	+	+	+	+	+	+	
32	+	+	+	+	+	+	+	+	+	+	+	+	+
33	+	+	+	+	+	+	+	+	+	+	+	+	
34	+	+	+	+	+	+	+	+	+	+	+	+	
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	
37	+		+	+	+	+	_	+	+	+	+	+	+
38	+	+	+	+	+	+	+	+	+	+	+	+	

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9 + + + + + +	_ _
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11 + + - + - + -	_
12 +	_
13 +	_
14 + + + + + + + + + + + + + + + + + + +	_
15 + + + + + + + + - + - +	_
16 + + + + + + + + + + + + + + + + + + +	_
17 + + + +	_
18 + + + + + + + + + + + + +	_
19 + + + + + + + + + + + +	+
20 + + + + + + + + + + + + + + + + + + +	_
21 + + + + + + + + + + + + +	_
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23 + + + + + + + + + + + + + +	_
24 + + +	_
25 + + + + + + + + + + + + + +	_
26 + + + + + + + + + + + + + +	_
27 + + + + + + + + + + + + + +	_
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31 + + +	_
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33 + + + + + + + + + + + + + +	+
34 + + + + + + + + + + + + + +	+
35 + + + + + + + + + + + + + +	+
36	_
37 + + + + + + + + + + + + + +	+
38 + + + + + + + + + + + + + +	+

Table 1 (Continued from previous page)

	\rightarrow_{40}	\rightarrow_{41}	\rightarrow_{42}	\rightarrow_{43}	\rightarrow_{44}	\rightarrow_{45}	\rightarrow_{46}	\rightarrow_{47}	\rightarrow_{48}	\rightarrow_{49}	\rightarrow_{50}	\rightarrow_{51}	\rightarrow_{52}
1	+	+	+	+	+	+	_	+	+	+	+	_	+
2	+	+	+	+	+	+	+	+	+	+	+		+
3	+	+	+	+	+	+	+	+	+	+	+	_	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	_	_	_	_	_	_	_	_	_	_	_	_	_
6	_	_	_	_	_	_	+	+	+	+	+	+	+
7	+	_	+	_	_	_	_	_	_	_	_	_	_
8	+	_	+	+	+	+	_	_	_	_	_	_	_
9	_	+	+	_	_	_	_	_	+	+	+	+	_
10	_	_	_	_	_	_	_	_	_	_	_	_	_
11	+	_	+	_	_	_	_	_	_	_	_	_	_
12	_	_	_	_	_	_	_	_	_	_	_	_	_
13	_	_	_	_	_	_	_	_	_	_	_	_	_
14	_	_	+	+	+	+	_	_	_	_	_	_	_
15	_	_	+	+	+	+	_	_	_	_	_	_	_
16	_	_	+	+	+	+	+	_	+	+	+	+	_
17	_	_	_	_	_	_	+	_	+	+	+	+	_
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	_	_	+	+	+	+	_	_	_	_	_	_	_
21	+	+	+	+	+	+	+	+	+	+	+	+	+
22	+	+	+	+	+	+	+	+	+	+	+	+	+
23	+	+	+	+	+	+	+	+	+	+	+	+	+
24	_	_	_	_	_	_	+	+	+	+	+	+	+
25	+	+	+	+	+	+	+	+	+	+	+	+	+
26	+	+	+	+	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28							+	+	+	+	+	+	+
29	_	_	_	_	_	_	+	_	+	+	+	+	_
30	+	_	+	+	+	+	+	+	+	+	+	+	+
31	_	_	_	_	_	_	+	_	+	+	+	+	
32	_	_	_	_	_	_	+	+	+	+	+	+	+
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	_
37	+	+	+	+	+	+	_	_	_	_	_	_	
38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

	\rightarrow_{53}	\rightarrow_{54}	\rightarrow_{55}	\rightarrow_{56}	\rightarrow_{57}	\rightarrow_{58}	\rightarrow_{59}	\rightarrow_{60}	\rightarrow_{61}	\rightarrow_{62}	\rightarrow_{63}	\rightarrow_{64}	\rightarrow_{65}
1	_	_	+	+	+	+	+	+	+	+	+	+	+
2	+	+	+	+	+	+	+	+		+	+	_	+
3	+	+	+	+	+	+	+	+	_	+	+	_	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	_	_	_	_	_	_	_	_	+	_	_	+	
6	+	+	+	+	_	+	+	_	+	_	_	+	
7	_	_	_	_	_	_	_	_	_	+	+	_	+
8	_	_	_	_	_	_	_	_	+	+	+	+	+
9	_	_	_	+	+	_	_	_	_	_	_	_	_
10	_	_	_	_	_	_	_	_	_	_	_	_	_
11	_	_	_	_	_	_	_	_	_	+	+	_	+
12	_	_	_	_	_	_	_	_	_	_	_	_	_
13	_	_	_	_	_	_	_	_	_	_	_	_	_
14	_	_	_	_	_	_	_	_	+	_	_	+	_
15	_	_	_	_	_	_	_	_	+	_	_	+	_
16	+	_	_	_	+	_	_	_	+	_	_	+	_
17	+	_	+	_	+	_	_	_	+	_	_	_	_
18	+	_	+	+	+	_	_	_	+	+	+	+	+
19	+	+	+	+	+	_	_	_	+	+	+	+	+
20	_	_	_	_	_	_	_	_	+	_	_	+	_
21	+	_	+	+	+	_	_	_	+	+	+	+	+
22	+	_	+	+	+	_	_	_	+	+	+	+	+
23	+	_	+	+	+	_	_	_	+	+	+	+	+
24	+		+	+	+				+	+		+	+
25	+		+	+	+	_			+			+	+
26	+	_	+	+	+	_	_	_	+	+	+	+	+
_27	+	_	+	+	+	_	_	_	+	+	+	+	+
28	+	_	+	+	+	_	_	_	+	+	+	+	+
29	+	_	+	_	+	_	_	_	+	_	_	_	
30	+	_	+		+	_	_	_	+	_	_	+	+
31	+	_	+	_	+	_	_	_	+	+	_	_	
32	+	_	+	+	+	_	_	_	+	_	_	_	
33	+	+	+	+	+	+	+	+	+	+	+	+	
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	
37	_	_	_	_	_	_	_	_	+	+	+	+	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

	\rightarrow_{66}	\rightarrow_{67}	\rightarrow_{68}	\rightarrow_{69}	\rightarrow_{70}	\rightarrow_{71}	\rightarrow_{72}	\rightarrow_{73}	\rightarrow_{74}	\rightarrow_{75}	\rightarrow_{76}	\rightarrow_{77}	\rightarrow_{78}
1	+	+	+	+	+	+	+	+	+	_	+	+	+
2	_	_	+	+	+	_	+	+	+	_	+	+	+
3	_	+	+	+	+	+	+	+	+	+	+	+	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	_	+	_	_	_	_	_	_	_	_	_	_	_
6	_	+	_	+	_	_	+	+	_	_	+	+	+
7	_	_	+	+	_	_	_	_	+	_	_	+	_
8	+	_	+	+	_	+	+	_	+	+	+	+	
9	_	_	_	_	_	_	_	_	+	_	+	+	_
10	_	_	_	+	_	_	_	_	_	_	_	_	_
11	_	_	+	+	_	_	_	_	+	_	_	+	
12	_	_	_	_	_	_	_	_	+	_	+	+	_
13	_	_	_	_	_	_	_	_	+	_	+	+	_
14	+	_	_	_	_	+	+	_	+	+	+	+	
15	+	_	_	_	_	+	_	_	+	+	+	+	
16	+	_	_	_	_	+	+	_	+	+	+	+	
17	+	_	_	_	_	+	_	_	+	+	+	+	_
18	+	_	+	+	_	+	+	_	+	+	+	+	
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	_	_	_	_	+	+	_	+	+	+	+	_
21	+	_	+	+	_	+	+	_	+	+	+	+	_
22	+	_	+	+	_	+	+	_	+	+	+	+	
23	+	_	+	+	_	+	+	_	+	+	+	+	_
24	+	_	_	_	_	+	+	_	+	+	+	+	_
25	+	_	_	_	_	+	+	_	+	+	+	+	_
26	+	_	+	+	_	+	+	_	+	+	+	+	
27	+	_	+	+	_	+	+	_	+	+	+	+	
28	+	_	+	+	_	+	+	_	+	+	+	+	
29	+	_	_	_	_	+	_	_	+	+	+	+	
30	+	_	_	_	_	+	+	_	+	+	+	+	
31	+	_	_	_	_	+	_	_	+	+	+	+	
32	+	_	_	_	_	+	_	_	+	+	+	+	
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	
37	+	+	+	_	+	+	_	_	+	+	_	_	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

1 +		\rightarrow_{79}	\rightarrow_{80}	\rightarrow_{81}	\rightarrow_{82}	\rightarrow_{83}	\rightarrow_{84}	\rightarrow_{85}	\rightarrow_{86}	\rightarrow_{87}	\rightarrow_{88}	\rightarrow_{89}	\rightarrow_{90}	\rightarrow_{91}
3 +	1													
3 +	2	+	+	+	_	+	+	_	_	+	+	+	+	
5 -	3	+	+	+	_	+	+	_	+	+	+	+	+	
6 + + + -	4	+	+	+	+	+	+	+	+	+	+	+	+	+
7 - - - + + -	5	_	_	_	_	_	_	_	_	_	_	_	_	_
8 + + + + + + + + + + -	6	+	+	+	_	_	_	_	_	_	_	_	_	+
9 + - + -	7	_	_	_	_	+	+	_	_	_	+	_	_	_
10 -	8	+	+	+	+	+	+	+	_	_	+	+	+	
11 - - - + + -	9	+	_	+	_	_	_	_	_	_	+	_	_	_
12 + -	10	_	_	_	_	_	_	_	_	_	_	_	_	_
13 + -	11	_	_	_	_	+	+	_	_	_	+	_	_	
14 + + + - + + + - + + - + + - + - + - + - + - + - + - + - + - + - + - + - +	12	+	_	_	_	_	_	_	_	_	_	_	_	_
15 + - + - - + - + - + - + - + - - + - - +	13	+	_	_	_	_	_	_	_	_	_	_	_	_
16 +	14	+	+	+	+	_	_	+	_	_	+	+	+	
17 + - - - - - - +	15	+	_	+	+	_	_	+	_	_	+	_	+	_
18 +	16	+	+	+	+	_	_	+	_	_	+	+	+	+
19 +	17	+	_	+	_	_	_	_	_	_	_	_	_	+
20 +	18	+	+	+	+	+	+	+	_	_	+	+	+	+
21 +	19	+	+	+	+	+	+	+	+	+	+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	20	+	+	+	+	_	_	+	_	_	+	+	+	_
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	21	+	+	+	+	+	+	+	_	_	+	+	+	+
24 + + + - - - - - - +	22	+	+	+	+	+	+	+	_	_	+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	23	+	+	+	+	+	+	+	_	_	+	+	+	+
26 +	24	+	+	+	_	_	_	_	_	_	_	_	_	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	25	+	+	+	+	+	_	+			+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	26	+	+	+	+	+	+	+	_	_	+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	27	+	+	+	+	+	+	+	_	_	+	+	+	+
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	28	+	+	+	_	_	_	_	_	_	_	_	_	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	29	+	_	+	_	_	_	_	_	_	_	_	_	+
32 + - + - - - - - - - - - + </th <th>30</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th>	30	+	+	+	+	_	_	+	_	_	+	+	+	+
33 + </th <th>31</th> <th>+</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>+</th>	31	+	_	+	_	_	_	_	_	_	_	_	_	+
34 + </th <th>32</th> <th>+</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>+</th>	32	+	_	+	_	_	_	_	_	_	_	_	_	+
35 + </th <th></th> <th>+</th> <th></th>		+	+	+	+	+	+	+	+	+	+	+	+	
36 - </th <th></th> <th>+</th>		+	+	+	+	+	+	+	+	+	+	+	+	+
37 + + + + + + + + + + + -		+	+	+	+	+	+	+	+	+	+	+	+	+
	36	_	_	_	_	_	_	_	_	_	_	_	_	
38 + + + + + + + + + + + + + +		+	+	+	+	+	+	+	+	+	+	+	+	
	38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

1 +		\rightarrow_{92}	\rightarrow_{93}	\rightarrow_{94}	\rightarrow_{95}	\rightarrow_{96}	\rightarrow_{97}	\rightarrow_{98}	\rightarrow_{99}	\rightarrow_{100}	\rightarrow_{101}	\rightarrow_{102}	\rightarrow_{103}	\rightarrow_{104}
2 + + - +	1													
3 +	2	+	+	_	_	+	+	+	+	+	+	+	+	
4 +	3				+									
6 +	4	+	+	+	+	+	+	+	+	+	+	+	+	+
7 -	5	_	_	_	_	_	_	_	_				_	
8 - - - - +	6	+	+	+	+	+	+	+	+	_	_	_	_	
9 -	7	_	_	_	_	_	_	_	_	_	_	_	_	
9 - - - + -	8	_	_	_	_	_	_	_	_	+	+	+	+	+
10 -	9	_	_	_	_	_	+	_	_	+				
12 -	10	_	_	_	_	_	_	_	_		_	_	_	
13 -	11	_	_	_	_	_	_	_	_	+	+	+	+	+
14 - - - - +	12	_	_	_	_	_	_	_	_	_	_	_	_	
15 - - - - +	13	_	_	_	_	_	_	_	_	_	_	_	_	_
16 - - + - - +	14	_	_	_	_	_	_	_	_	+	+	+	+	+
17 - - +	15	_	_	_	_	_	_	_	_	+	+	+	+	+
18 - +	16	_	_	+	_	_	+	_	_	+	+	+	+	+
19 - +	17	_	_	+	_	_	+	_	_	+	+	+	_	_
20 - - - - +	18	_	+	+	_	_	+	+	+	+	+	+	+	+
21 - + + - +	19	_	+	+	+	+	+	+	+	+	+	+	+	+
22 - + + - +	20	_	_	_	_	_	_	_	_	+	+	+	+	+
23 - + + - +	21	_	+	+	_	_	+	+	_	+	+	+	+	+
24 - - + - - + + + - +	22		+	+	_	_	+	+	_	+	+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	23	_	+	+	_	_	+	+	_	+	+	+	+	+
26 - + + - +	24	_	_	+	_	_	+	_	_	+	+	+	_	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	25	_		+			+			+	+	+	+	+
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	26	_	+	+	_	_	+	+	_	+	+	+	+	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	_27	_	+	+	_	_	+	+	+	+	+	+	+	+
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	28	_	+	+	_	_	+	_	_	+	+	+	_	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	29	_	_	+	_	_	+	_	_	+	+	+	_	
32 - - + </th <th>30</th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>+</th> <th>_</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th>	30	_	_	+	_	_	+	+	_	+	+	+	+	+
33 + </th <th>31</th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>+</th> <th>+</th> <th>_</th> <th></th>	31	_	_	+	_	_	+	_	_	+	+	+	_	
34 + </th <th></th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>_</th> <th>_</th> <th>+</th> <th>+</th> <th>+</th> <th>_</th> <th>+</th>		_	_	+	_	_	+	_	_	+	+	+	_	+
35 + </th <th></th> <th>+</th> <th></th>		+	+	+	+	+	+	+	+	+	+	+	+	
36 - - - - + + + + + + 37 - - - - - + + + + +		+	+	+	+	+	+	+	+	+	+	+	+	
37 + + + + +		+	+	+	+	+	+	+	+	+	+	+	+	+
		_	_	_	_	_	_	_	_	+	+	+	+	
38 + + + + + + + + + + + + + + +		_	_	_	_	_	_	_	_	+	+	+	+	+
	38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

		```			\								- vage)
1	$\rightarrow_{105}$				$\rightarrow$ 109	$\rightarrow$ 110		$\rightarrow_{112}$		$\rightarrow_{114}$	$\rightarrow_{115}$	$\rightarrow_{116}$	$\rightarrow_{117}$
1	+	+	+	+									
2	+	+	+	+	+	+		+		+	+		
3	+	_	_	+	+	+	+	+	_	+	+	+	
4	+	+	+	+	+	+	+	+	+	+	+	+	
5	_		_	_	+	+		+	_	_	_		
6	_	_	_	_	+	+	_	+	_	_	_	_	
	_	_	_	_	_	_	_	_	_	_	_	_	
8	+		_	_	+	+	+	+	+	+	+	+	+
9	_	_	_	_		+	_	+	_	_		_	
10	_	_	_	_	_	_	_	_	_	_	_	_	
11	+	+	+	+	_	_	_	_	_	_	_	_	_
12	_		_	_	_	_	_		_	_		_	
13	_	_	_	_	_	_	_	_	_	_	_	_	
14	+	_	_	_	+	+	+	+	+	+	+	+	+
15	+	_	_	_	+	+	+	+	+	+	+	+	+
16	+	+	+	_	+	+	+	+	+	+	+	+	+
17	_	+	_	_	+	+	+	+	+	_	_	_	_
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	_	+	_	+	+	+	+	+	+	+	+	+
21	+	_	+	_	+	+	+	+	+	+	+	+	+
22	+	_	+	_	+	+	+	+	+	+	+	+	+
23	+	+	+	_	+	+	+	+	+	+	+	+	+
24	+	_	_	_	+	+	+	+	+	_	_	_	+
25	+	+	+	_	+	+	+	+	+	+	+	+	+
26	+	+	+	_	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28	+	_	+	_	+	+	+	+	+	_	_	_	+
29	_	+	_	_	+	+	+	+	+	_	_	_	_
30	+	+	+	+	+	+	+	+	+	+	+	+	+
31	_	_	_	_	+	+	+	+	+	_	_	_	+
32	+	+	_	_	+	+	+	+	+	_	_	_	_
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	+	+	+	+	_	_	_	_	_	_	_	_	
37	+	+	+	+	+	+	+	+	+	+	+	+	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+
		*	•	•	•	*		•	•		*		-

Table 1 (Continued from previous page)

	$\rightarrow_{118}$	$\rightarrow$ 110	$\rightarrow$ 120	$\rightarrow$ 191	$\rightarrow_{122}$	$\rightarrow$ 199	$\rightarrow$ 124			$\rightarrow_{127}$	$\rightarrow_{128}$	$\rightarrow_{129}$	$\rightarrow_{130}$
1	- T10	- T19 -	- 120 -	- 121 -	- 122 	- 125 -	+	+	- 120 -	+	- 128	+	+
2	_	+	+	_	+								
3	_	+	+	+	<del></del>			+	+	+			+
4	+	+	+	+	<del></del>	+	+	+	+	+	+	+	+
5	_												
6	_	+	+		+								
7	_												_
8	+						+	+	+	+	+	+	+
9	_												
10	_												
11	_												
12	_	_	_	_				_	_				
13	_	_	_	_	_	_	_	_	_	_	_		
14	+		_	_		_	+	+	+	+	+	+	+
15	+	_	_	_	_		+	+	+	+	+	+	+
16	+	_	+	+	+	_	+	+	+	+	+	+	+
17	+	_	_	+	_	_	+	+	+	+	+	_	
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	_	_	_	_	_	+	+	+	+	+	+	+
21	+	+	+	+	+	+	+	+	+	+	+	+	+
22	+	+	+	+	+	+	+	+	+	+	+	+	+
23	+	+	+	+	+	+	+	+	+	+	+	+	+
24	+	_	+	+	+	_	+	+	+	+	+	_	_
25	+	_	+	+	+	_	+	+	+	+	+	+	+
26	+	+	+	+	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28	+	+	+	+	+	_	+	+	+	+	+	_	
29	+	_	_	+	_	_	+	+	+	+	+	_	_
30	+	+	+	+	+	_	+	+	+	+	+	+	+
31	+		_	+		_	+	+	+	+	+	_	
32	+	+	_	+	_	_	+	+	+	+	+	_	_
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	_
37	+	_	_	_	_	_	+	+	+	+	+	+	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

1         -         +         -         +         -         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		$\rightarrow$ 191	$\rightarrow$ 122	$\rightarrow$ 199	→194	→125	$\rightarrow$ 126	$\rightarrow$ 197			$\rightarrow_{140}$	$\rightarrow_{141}$	$\rightarrow_{142}$	$\frac{15 page}{\rightarrow_{143}}$
2         -         -         -         +         -         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -	1						- T30		, 130 —					
3         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -	-													
4         +         +         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		+												
5         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -	-			+								+		
6         -         -         -         -         +         +         +         -         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -														
7         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -												+		
8         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		_												
9         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		+		+	_	_						+		
10         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -														
11         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		_		_										
12         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -	$\overline{}$	_		_										
13         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		_		_										
14         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		_		_						_				
15         +         -         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		+	+	+						_	_			
16         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -					_					_	_	_	_	
17         -         +         -         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -			+		+	+	+	+	_					
18         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +         +														
19         +         +         +         +         +         +         +         +         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		+		+					_	_			_	
20         +         +         +         +         +         +         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -									+	_	_	_	_	
21       +       +       +       +       +       -       +       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -										_				
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	22	+	+	+	+	+	+	+	_	+	_	+	_	_
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	23	+	+	+	+	+	+	+	_	+	_	+	_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	24	_	+	+	+	+	+	+	_	_	_	_	_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	25	+	+	+	+	+	+	+	_	_	_	_	_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	26	+	+	+	+	+	+	+	_	_	_	+	_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	27	+	+	+	+	+	+	+	_	_	_	_	_	_
30       +       +       +       +       +       +       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -       -	28	_	+	+	+	+	+	+	_	_	_	_	_	_
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32     -     +     -     +     +     +     +     +     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     -     - </th <th>30</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th>	30	+	+	+	+	+	+	+	_	_	_	_	_	_
33     +     +     +     +     +     +     -     -       34     +     +     +     +     +     +     +     +     +       35     +     +     +     +     +     +     +     +     +	31	_	_	+	+	+	+	+	_	_	_	_	_	_
34     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     +     + </th <th>32</th> <th>_</th> <th>+</th> <th>_</th> <th>+</th> <th>+</th> <th>+</th> <th>+</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th> <th>_</th>	32	_	+	_	+	+	+	+	_	_	_	_	_	_
35 + + + + + + + + + + + + +	33	+	+	+	+	+	+	+	+	+	_	+	_	_
	34	+	+	+	+	+	+	+	+	+	+	+	+	_
26	35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	36	_	_	_	_	_	_	_	_	_	_	_	_	_
37 + + +	37	+	+	+	_	_	_	_	_	_	_	_	_	_
38 + + + + + + + + + - +	38	+	+	+	+	+	+	+	+	+	_	+	_	_

Table 1 (Continued from previous page)

	$\rightarrow_{144}$	→14F	$\rightarrow$ 146	→1.47	→140	→140	$\rightarrow$ 100		$\rightarrow_{168}$	$\rightarrow_{169}$	$\rightarrow_{170}$	$\rightarrow_{171}$	$\frac{13 page}{\rightarrow_{172}}$
1	- 144 -	7 145	+	+	+	+	7 100	7 167	7 168	7 169	7170	+	+
$\frac{1}{2}$			+	+	+	<del></del>	+	+	+	+	+	+	+
$\frac{2}{3}$							+	<u>'</u>	+	+	+	+	+
4			+	+	+	+	<u>'</u>	+	+	+	+	+	+
5							<del></del>						
6		+		+		+	+	+		+		+	+
7			_									+	<del></del>
8			+	+	+		+	+	+		+	+	+
9													
10													
11												+	+
12	_												
$\frac{12}{13}$	_												
14	_						+	+	+		+		
15			_				+	<del></del>	+		+		
16							<u>·</u>	+	+	+	<u>·</u>		
17							+	+		+	+		+
18			_	_			<u>·</u>	+	+	+	+	+	+
19	_		_	_			+	+	+	+	+	+	+
20	_	_	_	_	_	_	+	+	+		+		
21	_	_	+	+	+	+	+	+	+	+	+	+	+
22	_	_	+	+	+	+	+	+	+	+	+	+	+
23	_	_	+	+	+	+	+	+	+	+	+	+	+
24	_	_	_	_	_	_	+	+	_	+	+	+	+
25	_	_	_	_	_	_	+	+	+	+	+	+	+
26	_	_	+	+	+	+	+	+	+	+	+	+	+
27	_	_	_	_	_	_	+	+	+	+	+	+	+
28	_	_	_	_	_	_	+	+	_	+	+	+	+
29	_	_	_	_	_	_	+	+	_	+	+	_	+
30	_	_	_	_	_	_	+	+	+	+	+	+	+
31	_	_	_	_	_	_	+	+	_	+	+	_	+
32	_	_	_	_	_	_	+	+	_	+	+	+	+
33	_	_	+	+	+	+	+	+	+	+	+	+	+
34	+	_	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	_
37	_	_	+	_	+	_	+	_	+	_	+	_	_
38	_	_	+	+	+	+	+	+	+	+	+	+	+

Table 1 (Continued from previous page)

	$\rightarrow_{173}$	$\rightarrow_{174}$	$\rightarrow_{175}$	$\rightarrow_{176}$	$\rightarrow$ 177	$\rightarrow$ 178	$\rightarrow$ 170			$\rightarrow_{182}$	$\rightarrow_{183}$	$\rightarrow_{184}$	$\frac{15 \text{ page}}{\rightarrow_{185}}$
1	+	+	+	+	+	+	+	+	+	+	+	+	+
2	+	+	+	+	+	+	<u>·</u>	+	+	+	+	+	<del>`</del>
3	+	+	+	+	+	+	+	+	+	+	+	+	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+
5	_		_	+	_			_	+	_			
6	_	+	_	+	+	_	+	_	+	+	_	_	+
7	+	_	+	+	+	+	_	+	_	_	_	_	
8	+	_	+	+	+	+	_	+	_	_	_	_	
9	_	_	_	_	+	+	+	+	+	+	+	+	+
10	_	_	_	_	_	_	_	_	_	_	_	_	
11	+	_	+	+	+	+	_	+	_	_	_	_	
12	_	_	_	_	+	_	_	+	_	_	_	_	_
13	_	_	_	_	+	_	_	+	_	_	_	_	
14	_	_	_	+	+	+	_	+	_	_	_	_	_
15	_	_	_	+	+	+	_	+	_	_	_	_	_
16	_	_	_	+	+	+	+	+	_	_	_	_	_
17	_	+	+	_	+	_	+	+	_	_	_	_	_
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	_	_	_	+	+	+	_	+	_	_	_	_	_
21	+	+	+	+	+	+	+	+	+	+	+	+	+
22	+	+	+	+	+	+	+	+	+	+	+	+	+
23	+	+	+	+	+	+	+	+	+	+	+	+	+
24	_	+	+	+	+	_	+	+	+	+	_	+	+
25	+	+	+	+	+	+	+	+	+	+	+	+	+
26	+	+	+	+	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28	_	+	+	_	+	_	+	+	+	+	_	+	+
29	_	+	+	_	+	_	+	+	_	_	_	_	
30	+	+	+	+	+	+	+	+	_	_	_	_	
31	_	+	+	+	+	_	+	+	_	_	_	_	_
32	_	+	+	_	+	_	+	+	+	+	_	+	+
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	+	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
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36	_	_	_										
36 37 38	_ +	_	+	+	_	+	_	+	+	_	+	+	

Table 1 (Continued from previous page)

		$\rightarrow_{187}$	, TQQ	-7189	$\rightarrow_{190}$	$\rightarrow_{191}$	$\rightarrow_{192}$	$\rightarrow_{193}$	$\rightarrow_{194}$	$\rightarrow_{195}$	$\rightarrow_{196}$	$\rightarrow_{197}$	$\rightarrow_{198}$
1	$\frac{\rightarrow_{186}}{+}$	+	+	+	+	_	+	+	+	+	+	+	+
2	+	+	+	+	+	+	_	_	_	_	_	_	
3	+	+	+	+	+	+	_	_	_	_	_		
4	+	+	+	+	+	+	+	_	+	+	+	+	+
5	_	_	_	_	_	_	+	_	_	_	_	_	
6	_	_	_	+	_	+	+	+	_	+	_	+	_
7	+	+	+	_	+	+	_	_	_	_	_	_	_
8	+	+	+	_	+	+	+	_	+	+	+	_	+
9	_	+	+	+	+	_	_	_	_	_	_	_	_
10	_	_	_	_	_	_	_	_	_	_	_	_	
11	+	+	+	_	+	+	_	_	_	_	_	_	_
12	_	+	_	_	+	_	_	_	_	_	_	_	_
13	_	+	_	_	+	_	_	_	_	_	_	_	_
14	+	+	+	_	+	+	+	_	+	+	+	_	+
15	+	+	+	_	+	+	+	_	+	+	+	_	+
16	+	+	+	+	+	_	+	_	+	+	+	+	+
17	_	+	_	+	+	_	+	_	_	+	_	+	+
18	+	+	+	+	+	+	+	+	+	+	+	+	+
19	+	+	+	+	+	+	+	+	+	+	+	+	+
20	+	+	+	_	+	+	+	_	+	+	+	_	+
21	+	+	+	+	+	+	+	+	+	+	+	+	+
22	+	+	+	+	+	+	+	+	+	+	+	+	+
23	+	+	+	+	+	+	+	+	+	+	+	+	+
24	+	+	_	+	+	+	+	+	_	+	_	+	+
25	+	+	+	+	+	+	+	+	+	+	+	+	+
26	+	+	+	+	+	+	+	+	+	+	+	+	+
27	+	+	+	+	+	+	+	+	+	+	+	+	+
28	+	+	_	+	+	+	+	+	_	+	_	+	+
29	_	+	_	+	+	_	+	_	_	+	_	+	+
30	+	+	+	+	+	_	+	_	+	+	+	+	+
31	+	+	_	+	+	_	+	+	_	+	_	+	+
32	_	+	_	+	+	+	+	+	_	+	_	+	+
33	+	+	+	+	+	+	+	+	+	+	+	+	+
34	+	+	+	+	+	+	+	_	+	+	+	+	+
35	+	+	+	+	+	+	+	+	+	+	+	+	+
36	_	_	_	_	_	_	_	_	_	_	_	_	_
37	+	+	+	_	+	_	+	_	+	_	+	_	+
38	+	+	+	+	+	+	+	+	+	+	+	+	+

# 3 Shortlisting the most suitable intuitionistic fuzzy implications

In this research, we are specifically interested to outline which of all the 182 implications in the table (from  $\rightarrow_1$  to  $\rightarrow_{149}$  and from  $\rightarrow_{160}$  to  $\rightarrow_{198}$ ) are most appropriate to work with in practice. We define this implication's usability as the property to satisfy the largest number of axioms (objective, quantifiable criterion), and—in addition—with the most concise record that is easy to work with (secondary, more subjective but not less important criterion).

To get a "bird-eye" impression of the implications' satisfying of the axioms, we give the Figure 1 which is another way of presenting the information from Table 1, where all satisfied axioms ("+") are marked in red and all unsatisfied axioms ("-") are marked in blue. The axioms sorted by the number of implications that satisfy them is given in the form of a histogram in the next Figure 2.

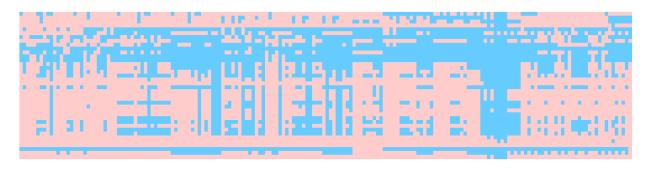


Figure 1. The total list of 182 implications (columns) by the 38 implications (rows), with the satisfied axioms ("+") marked in red and the unsatisfied axioms ("-") marked in blue.

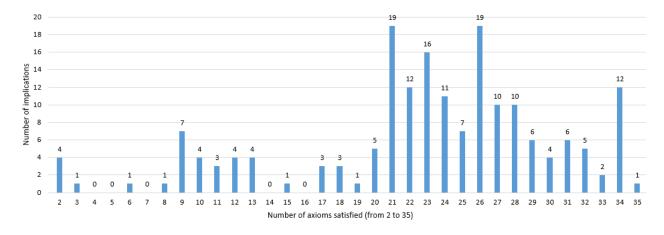


Figure 2. The number of implications per number of satisfied axioms (up to 35 out of 38)

Starting from the highest number of satisfied axioms per implication (that is, starting from the rightmost part of histogram of Figure 2), we selected the upper quartile, top 25% or the 44 implications (per the Remark in Section 2, implications  $\rightarrow_{187}$ ,  $\rightarrow_{190}$  are to be excluded, so the total number of 46 is reduced to 44), which satisfy at least 28 out of 38 axioms. Alternatively, selecting the top decile, that is approximately the top 20 implications that satisfy at least 32 out of 38 axioms, is considered rather restrictive, but in some cases it may be a valid option.

These 44 implications we call "suitable" implications, and we are listing them below with the number of satisfied axioms each, sorted in decreasing order:

1 implication satisfying 35 axioms:  $\rightarrow_{14}$ 

```
10 \text{ implications satisfying } 34 \text{ axioms: } \rightarrow_3, \rightarrow_4, \rightarrow_5, \rightarrow_{11}, \rightarrow_{13}, \rightarrow_{23}, \rightarrow_{74}, \rightarrow_{77}, \rightarrow_{177}, \rightarrow_{180}, \rightarrow_{11}, \rightarrow_{12}, \rightarrow_{13}, \rightarrow_{14}, \rightarrow_{15}, \rightarrow_{11}, \rightarrow_{12}, \rightarrow_{13}, \rightarrow_{14}, \rightarrow_{15}, \rightarrow_{11}, \rightarrow_{12}, \rightarrow_{13}, \rightarrow_{14}, \rightarrow_{17}, \rightarrow_{180}, \rightarrow_{
```

- 2 implications satisfying 33 axioms:  $\rightarrow_{20}$ ,  $\rightarrow_{79}$ ,
- 5 implications satisfying 32 axioms:  $\rightarrow_{18}, \rightarrow_{22}, \rightarrow_{27}, \rightarrow_{28}, \rightarrow_{76},$
- 6 implications satisfying 31 axioms:  $\rightarrow_{17}$ ,  $\rightarrow_{81}$ ,  $\rightarrow_{100}$ ,  $\rightarrow_{102}$ ,  $\rightarrow_{110}$ ,  $\rightarrow_{112}$ ,
- 3 implications satisfying 30 axioms:  $\rightarrow_{101}, \rightarrow_{109}, \rightarrow_{166},$
- 7 implications satisfying 29 axioms:  $\rightarrow_1, \rightarrow_9, \rightarrow_{24}, \rightarrow_{29}, \rightarrow_{61}, \rightarrow_{176}, \rightarrow_{192},$
- $10 \text{ implications satisfying } 28 \text{ axioms: } \rightarrow_2, \rightarrow_{35}, \rightarrow_{71}, \rightarrow_{105}, \rightarrow_{125}, \rightarrow_{127}, \rightarrow_{167}, \rightarrow_{170}, \rightarrow_{186}, \rightarrow_{198}.$

These implications are given in Table 2.

Table 2. List of the suitable intuitionistic fuzzy implications

$\rightarrow_1$	$\langle \max(b, \min(a, c)), \min(a, d) \rangle$
$\rightarrow_2$	$\langle \overline{\operatorname{sg}}(a-c), d\operatorname{sg}(a-c) \rangle$
$\rightarrow_3$	$\langle 1 - (1-c)\operatorname{sg}(a-c)\rangle, d\operatorname{sg}(a-c)\rangle$
$\rightarrow_4$	$\langle \max(b,c), \min(a,d) \rangle$
$\rightarrow_5$	$\langle \min(1, b+c), \max(0, a+d-1) \rangle$
$\rightarrow_9$	$\langle b + a^2c, ab + a^2d \rangle$
$\rightarrow_{11}$	$\langle 1 - (1-c)\operatorname{sg}(a-c), d\operatorname{sg}(a-c)\operatorname{sg}(d-b) \rangle$
$\rightarrow_{13}$	$\langle b+c-bc,ad \rangle$
$\rightarrow_{14}$	$\langle 1 - (1-c)\operatorname{sg}(a-c) - d\operatorname{\overline{sg}}(a-c)\operatorname{sg}(d-b), d\operatorname{sg}(d-b) \rangle$
$\rightarrow_{17}$	$\langle \max(b,c), \min(ab+a^2,d) \rangle$
$\rightarrow_{18}$	$\langle \max(b,c), \min(1-b,d) \rangle$
$\rightarrow_{20}$	$\langle \max(\overline{sg}(a), sg(c)), \min(sg(a), \overline{sg}(c)) \rangle$
$\rightarrow_{22}$	$\langle \max(b, 1-d), 1 - \max(b, 1-d) \rangle$
$\rightarrow_{23}$	$\langle 1 - \min(\operatorname{sg}(1-b), \overline{\operatorname{sg}}(1-d)), \min(\operatorname{sg}(1-b), \overline{\operatorname{sg}}(1-d)) \rangle$
$\rightarrow_{24}$	$\langle \overline{\operatorname{sg}}(a-c) \overline{\operatorname{sg}}(d-b), \operatorname{sg}(a-c) \operatorname{sg}(d-b) \rangle$
$\rightarrow_{27}$	$\langle \max(\overline{sg}(1-b), sg(c)), \min(sg(a), \overline{sg}(1-d)) \rangle$
$\rightarrow_{28}$	$\langle \max(\overline{sg}(1-b), c), \min(a, d) \rangle$
$\rightarrow_{29}$	$\langle \max(\overline{sg}(1-b), \overline{sg}(1-c)), \min(a, \overline{sg}(1-d)) \rangle$
$\rightarrow_{35}$	$\langle 1 - ad, ad \rangle$
$\rightarrow_{61}$	$\langle \max(c, \min(b, d)), \min(a, d) \rangle$
$\rightarrow_{71}$	$\langle \max(b,c), \min(cd+d^2,a) \rangle$
$\rightarrow_{74}$	$\langle \max(\operatorname{sg}(b), \overline{\operatorname{sg}}(d)), \min(\overline{\operatorname{sg}}(b), \operatorname{sg}(d)) \rangle$
$\rightarrow_{76}$	$\langle \max(c, 1-a), \min(1-c, a) \rangle$
$\rightarrow_{77}$	$\langle (1 - \min(\overline{sg}(1-a), sg(1-c))), \min(\overline{sg}(1-a), sg(1-c)) \rangle$
	(Continued on next page)

(Continued on next page)

Table 2 (Continued from previous page)

$\rightarrow_{79}$	$\langle \max(\overline{sg}(1-c), sg(b)), \min(sg(d), \overline{sg}(1-a)) \rangle$
$\rightarrow_{81}$	$\langle \max(\overline{sg}(1-b), \overline{sg}(1-c)), \min(d, \overline{sg}(1-a)) \rangle$
$\rightarrow_{100}$	$\langle \max(b \operatorname{sg}(a), c), \min(a \operatorname{sg}(b), d) \rangle$
$\rightarrow_{101}$	$\langle \max(b \operatorname{sg}(a), c \operatorname{sg}(d)), \min(a \operatorname{sg}(b), \operatorname{sg}(c)d) \rangle$
$\rightarrow_{102}$	$\langle \max(b, c \operatorname{sg}(d)), \min(a, \operatorname{sg}(c)d) \rangle$
$\rightarrow_{105}$	$\langle \max(1-a, \min(1-d, \operatorname{sg}(d))), \min(a, d, \operatorname{sg}(1-d)) \rangle$
$\rightarrow_{109}$	$\langle b + \min(\overline{sg}(1-a), c), ab + \min(\overline{sg}(1-a), d)) \rangle$
$\rightarrow_{110}$	$\langle \max(b,c), \min(ab + \overline{sg}(1-a), d) \rangle$
$\rightarrow_{112}$	$\langle b+c-bc, ab+\overline{\mathrm{sg}}(1-a)d\rangle$
$\rightarrow_{125}$	$\langle \max(b, c), \min(cd + \overline{sg}(1 - d), a) \rangle$
$\rightarrow_{127}$	$\langle b+c-bc, (cd+\overline{sg}(1-d))a\rangle$
$\rightarrow_{166}$	$\langle \max(b, \min(a, c)), \min(a, \max(b, d)) \rangle$
$\rightarrow_{167}$	$\langle \max(1-a, \min(a, c)), \min(a, 1 - \min(a, c)) \rangle$
$\rightarrow_{170}$	$\langle \max(b, \min(1-b, 1-d)), 1 - \max(b, \min(1-b, 1-d)) \rangle$
$\rightarrow_{176}$	$\langle \overline{\operatorname{sg}}(a-c) + \operatorname{sg}(a-c) \max(b,c), \operatorname{sg}(a-c) \min(a,d) \rangle$
$\rightarrow_{177}$	$\langle \overline{\operatorname{sg}}(a-c) + \operatorname{sg}(a-c) \max(1-a,c), \operatorname{sg}(a-c) \min(a,1-c) \rangle$
$\rightarrow_{180}$	$\langle \overline{\operatorname{sg}}(d-b) + \operatorname{sg}(d-b) \max(b, 1-d), \operatorname{sg}(d-b) \min(1-b, d) \rangle$
$\rightarrow_{186}$	$\langle \overline{\operatorname{sg}}(d-b) + \operatorname{sg}(d-b) \max(b,c), \operatorname{sg}(d-b) \min(a,d) \rangle$
$\rightarrow_{192}$	$\langle \max(c, \min(b, d)), \min(d, \max(a, c)) \rangle$
$\rightarrow_{198}$	$\langle \max(1-d, \min(b, d)), 1 - \max(1-d, \min(b, d)) \rangle$

Finally, in Figure 3, an oriented graph is shown, with nodes corresponding to the different implications and oriented arcs where the top-down location of the nodes reflects the order from stronger to weaker impications. The nodes in the figure that correspond to implications  $\rightarrow_{20}, \rightarrow_{27}, \rightarrow_{29}, \rightarrow_{35}, \rightarrow_{74}, \rightarrow_{79}, \rightarrow_{81}, \rightarrow_{100}, \rightarrow_{101}, \rightarrow_{102}, \rightarrow_{105}$  are omitted, because they are not connected with any other nodes.

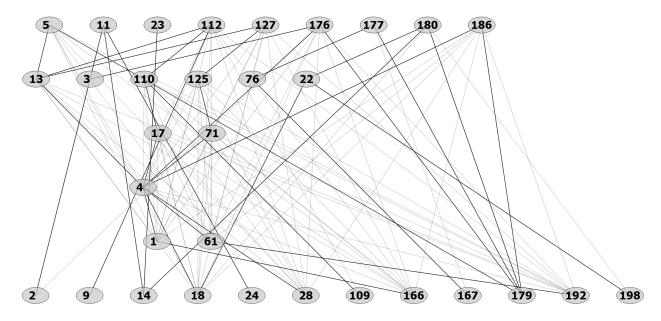


Figure 3. Oriented graph depicting the connections between the "suitable" implications.

#### 4 Conclusion: ideas for the future

In future, we will prepare a similar graph for all intuitionistic fuzzy implications that can potentially find real applications, e.g. in the intuitionistic fuzzy sets-based approach of InterCriteria Analysis, in decision-support systems, Data Mining tools, PROLOG-type languages, and others.

In [3] we started study the properties of the intuitionistic fuzzy negations. In the next research, we will continue the research initiated here, but for the case of negations. Finally, one more idea for future research is to look at the presented data from the axioms perspective and assess which of them are least and most satisfied and what conclusions regarding the intuitionistic fuzzy implications can be made in this regard.

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