

**APPLICATION OF INTUITIONISTIC FUZZY GENERALIZED
NETS FOR FLOWSHEETING SYSTEM SIMULATION***

S. Danev¹, G. Toneva², P. Georgiev³, V. Radeva⁴

1-University of Chemical and Metallurgical Technology - Sofia

2-University of Chemical and Metallurgical Technology - Sofia

3-Bulgarian Academy of Sciences, E-mail: prg@bgcict.acad.bg

4-Bulgarian Academy of Sciences, E-mail: valia@bgcict.acad.bg

1. Introduction

The Intuitionistic Fuzzy Generalized Nets (IFGN) [1] are an appropriate tool for modeling of real events, phenomenon and complex structures because of their flexibility and universal modeling possibilities. IFGNs allow description of both dynamic and static behavior of complex systems. The main advantage of using the IFGNs is the possibility for fast simulation of various system with complex structure - with sequential, parallel or recycle elements. It makes the IFGNs very suitable tool for mathematical modeling of technological system with large number of units and recycling material and energy streams.

The most of real industrial systems are complex technological systems having grate number of process units, interconnected by many sequential, bypass and recycle streams. Simulation of such complex systems is accomplished by preliminary decomposition of the entire system into a sequence of smaller subsystems. The calculation of these subsystems needs preliminary created computational modules for each process unit. The systems, having at least one recycle stream, require multiply calculations of the computational modules in iteration mode until convergence of so called cut streams is achieved.

Obviously to solve any optimization or control problems of such complex technological system is a time consuming task. Especially, when analytical type of unit models are used, it makes almost impossible to perform the simulation of the overall systems in real time.

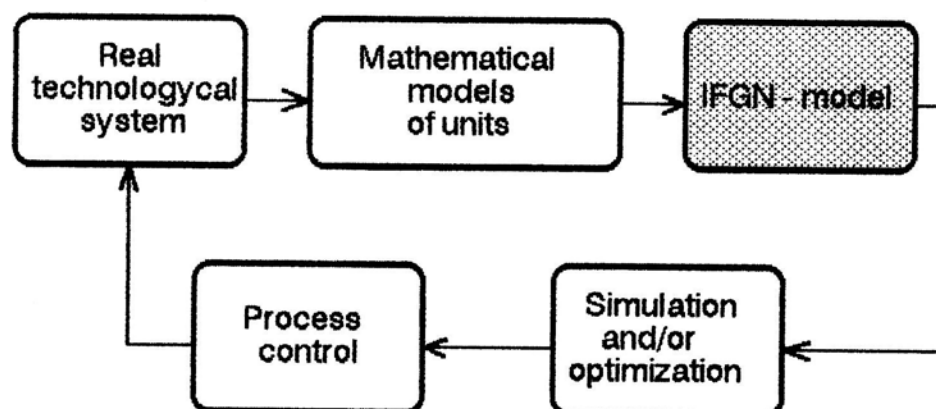


Fig.1

* This publication is financed from research project No TN-503 (HTMU 731)

An application of IFGN for static simulation of complex technological system, known as flowsheeting, is described in this paper.

The general scheme of the IFGN application in chemical technology is presented in Fig.1.

2. Intuitionistic Fuzzy Generalized Nets in Technological Systems.

A GN has static structure, made up of transitions, and dynamic elements - tokens, time component (related to the beginning, duration and elementary time-step of the modeled process), and memory, which accumulates information on the way of the process flow. Each transition has a set of input and a set of output places; pre-set conditions that must be satisfied in order to the token be able to transfer from the input to the output places; conditions of which the transition becomes active; and some other parameters. Tokens enter (or already are in) into IFGN with some initial characteristics and receive new characteristics while moving from place to place.

Up to now the GNs have not been applied for simulation of complex technological systems with recycling streams. Some investigations on use of IFGNs for energy and material balances calculations in refinery industry and for modeling of urea production are published in [2].

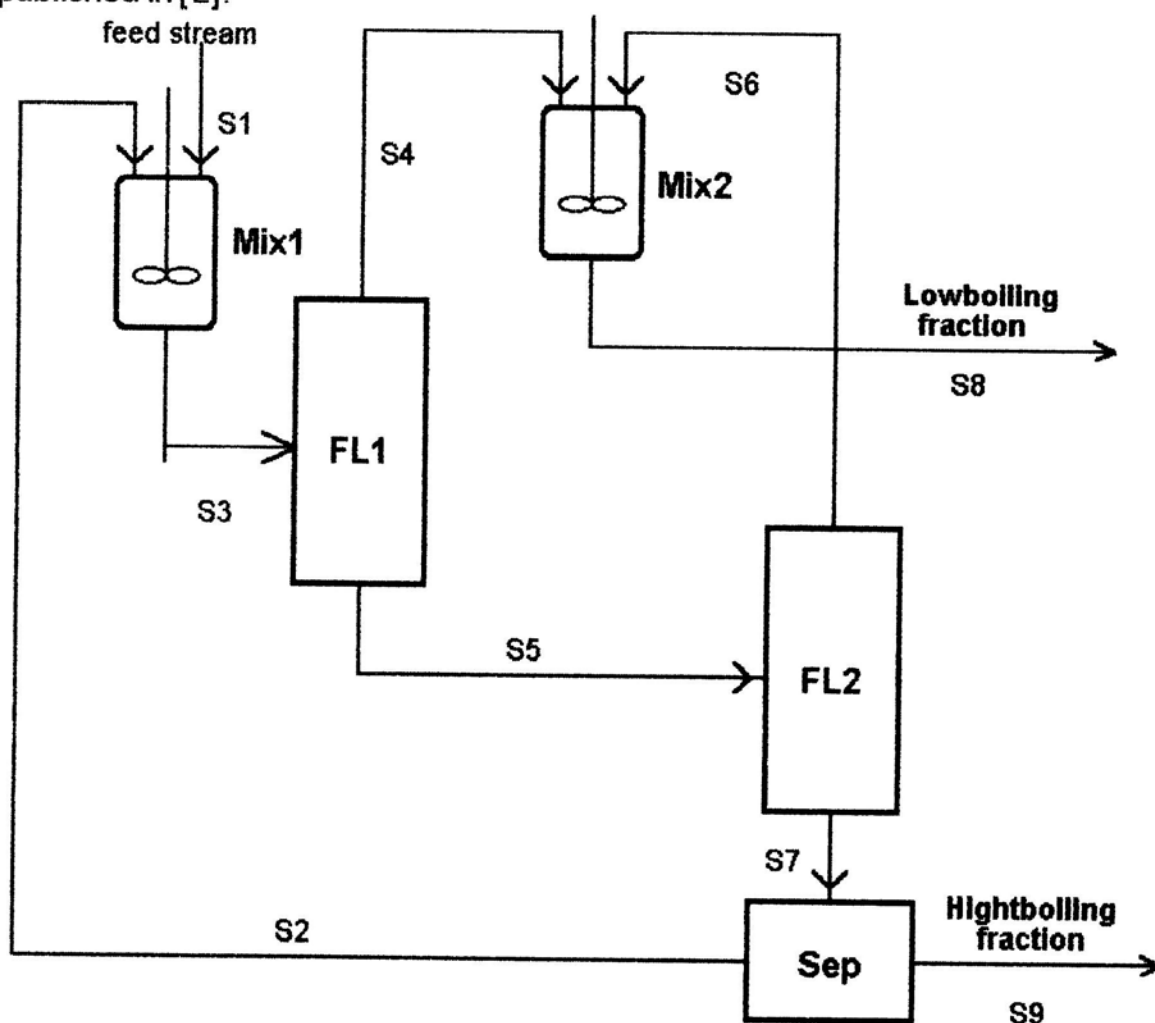


Fig.2

3. Description of the Flowsheeting System

A test continuous flowsheeting system with 9 streams and 5 technological units is presented in Fig.2. A 3-component mixture of butane (C₄H₁₀), heptane (C₇H₁₆) and octane (C₈H₁₈) is mixed in the unit Mix1 (streams S1 and S2) and enters the first flash unit FL1 (stream S3). At boiling temperature, two fractions are separated: the top lowboiling fraction (stream S4) and the bottom highboiling fraction (stream S5). The bottom fraction is secondary evaporated in FL2. The both top products from FL1 and FL2 (streams S4 and S6) are mixed in Mix2 and leave the system as product stream S8. The bottom product of FL2 (stream S7) enters the separator (Sep) where is divided into two streams: stream S9 as the system heavy product and stream S2 as a system recycling stream. It is used as a cut stream during the iterative calculations.

Strong analytical models are developed for every unit of the system and are organized as executable program modules.

The modules of FL1 and FL2 are identical and describe the flash process at boiling temperature. The mathematical description includes the following relationships [3]:

- equations of component material balances

$$F x_i - L x_i^L - V x_i^V = 0, \quad (i = 1, 2, \dots, N_c); \quad (1)$$

- equations of energy balance

$$F h_i - L h_i^L - V h_i^V = 0, \quad (i = 1, 2, \dots, N_c); \quad (2)$$

- vapor-liquid equilibrium equations

$$\sum x_i^L K_i - \sum x_i^V = 0, \quad (i = 1, 2, \dots, N_c) \quad (3)$$

where:

F is flowrate of the feed stream, [kmol/h];

N_c - number of components;

L, V - flowrate of the liquid and vapor phase, [kmol/h];

x_i^L, x_i^V - mole fraction of i-th component in liquid and vapor phase;

K_i - equilibrium constant of i-th component;

The solution of the above set of non-linear equations imposes an inner loop iterative procedure, that creates some computational difficulties in simulation of a complex structure with great number of process units.

The models of the mixers (Mix1 and Mix2) calculate the resulting output streams. The separator model (Sep) works with a specified separation coefficient.

4. Use of Generalized Net for the Flowsheeting System Simulation

The scheme of the GN for the above described Flowsheet simulation is shown in Fig.3. GN model consists of 5 transitions and 9 places. The transitions are marked with r1, r2, r3, r4, and, r5, as r1 and r4 describe Mix1 and Mix2; r2 and r3 describe FL1 and FL2; r5 - separator. Every token has initial or current characteristics in the form of *f1k, f2k,

f_{3k} (corresponding to the 1, 2, 3 component flowrate of the k -th stream). At every transfer the above characteristics receive current values. At every moment a token enters place I1 if it is empty, that symbolizes the input feed stream (S1). It goes to place I3 where it unites with the token arrived from I2. At initial moment of functioning of the GN the characteristics of the token in place I2 have approximate values, that symbolizes the recycling stream S2. The united token corresponds to stream S3. It splits into two tokens: one goes into place I4 (symbolizing S4) and the other - into place I5 (symbolizing S5). The token from place I5 splits into two tokens - one goes into place I6 (S6) and the other into I7 (S7). The tokens from places I4 and I6 are united in place I8, that corresponds to output product stream (S8).

The token from place I7 splits into two tokens - one goes into I9 (symbolizing the output product stream S9) and the other comes back into place I2. In the end of the process, the final characteristics of the tokens from places I8 and I9 are checked up.

The presence of one recycling stream (S2 at Fig.2) imposes iteration process that continues until the flowrate's parameters of the cut stream converge to the predefined value (about 10 iterations). The GN must function at least 50 takts, assuming that every step in the net is realized in one takt. For simplicity, it can be assumed that every transition is activated at every moment of time and has duration one unit of time. All places, transitions and arcs have equal capacity and priority.

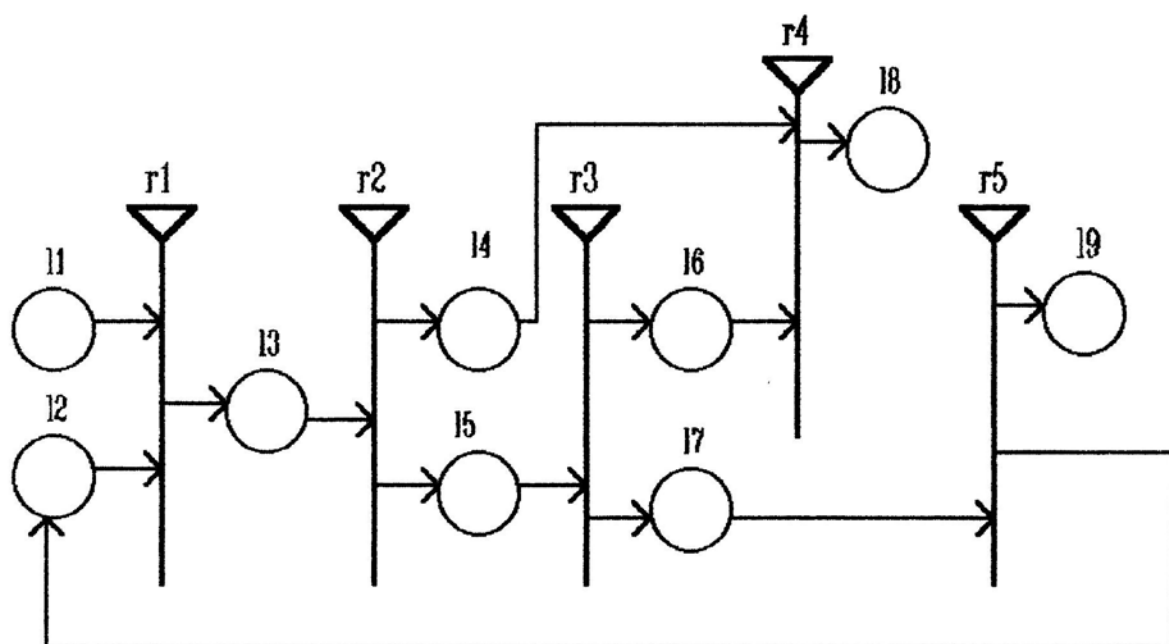


Fig.3

There are specifics in real processes that we most consider in our model. This is usually a very hard problem to solve. The use of IFGN is extremely suitable for such cases.

Let the token that enters place I1 has as initial characteristic the pairs $\langle \mu_{x1,s1}, v_{x1,s1} \rangle$, $\langle \mu_{x2,s1}, v_{x2,s1} \rangle$, $\langle \mu_{x3,s1}, v_{x3,s1} \rangle$, d_{s1} where $\mu_{xi,s1}$, $v_{xi,s1}$, ($i=1, 2, 3$), $\mu_{xi,s1} + v_{xi,s1} \leq 1$ and $\mu_{xi,s1}$ represents the minimal mass percent of component i in the entering stream S1 for which we can guarantee, that it will enter the IFGN, $v_{xi,s1}$ represents the maximal mass

percent of component i in the entering stream $S1$ for which we can give the same guarantees and d_{s1} is debit of the stream $S1$.

The token that enters place $I2$ has as initial characteristic the pairs $\langle \mu_{x1,s2}, v_{x1,s2} \rangle$, $\langle \mu_{x2,s2}, v_{x2,s2} \rangle$, $\langle \mu_{x3,s2}, v_{x3,s2} \rangle$, d_{s2} where $\mu_{xi,s2}, v_{xi,s2}$, ($i=1, 2, 3$), $\mu_{xi,s1} + v_{xi,s1} \leq 1$ and μ_{s2} represents the minimal mass percent of component i in the is carried by stream $S2$ for which we can guarantee, that it will be obtained by previous cycle of functioning of the IFGN, $v_{xi,s1}$ represents the maximal mass percent of component i in the entering stream $S2$ for which we can give the same guarantees and d_{s1} is debit of the stream $S2$. We must note that only the initial values of $\mu_{xi,s2}$ and $v_{xi,s2}$ ($i=1,2,3$) are gained this way, all subsequent values are calculated in the process of functioning of the IFGN.

Two entry streams are mixed together in $Mix1$ that is represented by transition $r1$. The result is obtained in place $I3$. Its characteristics are determined by the characteristic function of the IFGN and they are of the following type

$$\begin{aligned}\mu_{xi,s3} &= F_{s3}(\mu_{xi,s1}, d_{s1}, \mu_{xi,s2}, d_{s2}), \\ v_{xi,s3} &= G_{s3}(v_{xi,s1}, d_{s1}, v_{xi,s2}, d_{s2}), \text{ where } \mu_{xi,s3} + v_{xi,s3} \leq 1, (i=1,2,3), \\ d_{s3} &= d_{s1} + d_{s2}.\end{aligned}$$

Where F_{s3} is a function that calculates the current value of minimal guaranteed amount of all components (x_1, x_2, x_3) in stream $S3$ on the base of input characteristics of these components in the streams $S1$ and $S2$ and current technological conditions, and G_{s3} is a function that calculates the current value of maximal guaranteed amount of all components (x_1, x_2, x_3) in stream $S3$ on the same base.

On the next step the token enters place $I4$, passing through the transition $r2$ which represents first flash unit $FI1$. Here the input substance is divided on two and the new characteristics are determined in the following way:

$$\begin{aligned}\mu_{xi,s4} &= F_{s4}(\mu_{xi,s3}, d_{s3}), \\ v_{xi,s4} &= G_{s4}(v_{xi,s3}, d_{s3}), \text{ where } \mu_{xi,s4} + v_{xi,s4} \leq 1, \\ d_{s4} &= h_{s3} * d_{s3}, \\ \mu_{xi,s5} &= F_{s5}(\mu_{xi,s3}, d_{s3}), \\ v_{xi,s5} &= G_{s5}(v_{xi,s3}, d_{s3}), \text{ where } \mu_{xi,s5} + v_{xi,s5} \leq 1, (i=1,2,3), \\ d_{s5} &= (1-h_{s3}) * d_{s3}.\end{aligned}$$

Where F_{s4} and G_{s4} are analogous to F_{s3} and G_{s3} , but they are calculated only on the base of characteristics of the input stream $S3$ and current technological conditions at that moment and h_{s3} is a coefficient of division of the stream $S3$.

By analogy we proceed further on the IFGN, transition by transition and on every step we calculate the new values on the base of the input characteristics. The above describes transitions are basic for this IFGN. We can use similar functions for all transitions of these types.

If the transition is from type 1 (two input places and one output place) the general form of the functions, which determine the characteristics of the token in the output place is:

$$\begin{aligned}\mu_{xi,sj} &= F_{sj}(\mu_{xi,sj-1}, d_{sj-1}, \mu_{xi,sj-2}, d_{sj-2}), \\ v_{xi,sj} &= G_{sj}(v_{xi,sj-1}, d_{sj-1}, v_{xi,sj-2}, d_{sj-2}), \text{ where } \mu_{xi,sj} + v_{xi,sj} \leq 1, (i=1,2,3), \\ d_{sj} &= d_{sj-1} + d_{sj-2},\end{aligned}$$

Or in other words, the characteristics in the output place depend on the characteristics of the input streams S_{j-1} and S_{j-2} and the current technological conditions.

If the transition is from type 2 (one input place and two output places) the general form of the functions, which determine the characteristics of the token in the output places is:

$$\begin{aligned}\mu_{xi, sj-1} &= F_{sj-1}(\mu_{sj}, d_{sj}), \\ v_{sj-1} &= G_{sj-1}(v_{xi, sj}, d_{sj}), \text{ where } \mu_{xi, sj-1} + v_{xi, sj-1} \leq 1, (i=1,2,3), \\ d_{sj-1} &= h_{sj} * d_{sj}, \\ \mu_{sj-2} &= F_{sj-2}(\mu_{sj}, d_{sj}), \\ v_{xi, sj-2} &= G_{sj-2}(v_{sj}, d_{sj}), \text{ where } \mu_{xi, sj-2} + v_{xi, sj-2} \leq 1, (i=1,2,3), \\ d_{sj-1} &= (1-h_{sj}) * d_{sj}.\end{aligned}$$

Or in other words, the characteristics in the output places depend on the characteristics of the input stream s_j and the current technological conditions.

The result is that in places 18 and 19 we obtain tokens with calculated characteristics, that show the limits in which each component will be represented in the output stream and on the base of this knowledge we can make conclusions about the influence of the technological conditions and in some extend predict and control the real process.

5. Conclusions

In this paper a method for simulation of complex technological systems by use of GNs is proposed, because of the flexible properties of the IFGN. The results show a very good possibility of the IFGN to simulate various technological systems with recycling structure.

References

1. Atanassov, K., Generalized Nets, World Scientific, Singapore, 1991.
2. Atanassov, K., (Ed.) Applications of Generalized Nets, World Scientific, Singapore, 1993.
3. Gani, R., G. Toneva, Simultaneous Steady-state and Dynamic Simulation of Chemical Processes, ffComp. Chem. Eng., V.13, No 415, pp. 563-570, 1989.

□