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## Contents

Part I: Counting and Aggregation
Intelligent Counting - Methods and Applications ..... 3
Maciej Wygralak
Recommender Systems and BOWA Operators ..... 11
Przemystaw Grzegorzewski, Hanna Łqcka
Aggregation Process and Some Generalized Convexity and Concavity ..... 23
Barbara Pękala
Some Class of Uninorms in Interval Valued Fuzzy Set Theory ..... 33
Pawet Drygaś
The Modularity Equation in the Class of 2-uninorms ..... 45
Ewa Rak
Part II: Linguistic Summaries Counting and Aggregation
Dealing with Missing Information in Linguistic Summarization: A Bipolar Approach ..... 57
Guy De Tré, Mateusz Dziedzic, Daan Van Britsom, Stawomir Zadrożny
Evaluation of the Truth Value of Linguistic Summaries - Case with Non-monotonic Quantifiers ..... 69
Anna Wilbik, Uzay Kaymak, James M. Keller, Mihail Popescu
Using Ant Colony Optimization and Genetic Algorithms for the Linguistic Summarization of Creep Data ..... 81
Carlos A. Donis-Díaz, Rafael Bello, Janusz Kacprzyk
Part III: Multicriteria Decision Making and Optimization
InterCriteria Decision Making Approach to EU Member States Competitiveness Analysis: Temporal and Threshold Analysis ..... 95
Vassia Atanassova, Lyubka Doukovska, Deyan Mavrov, Krassimir T. Atanassov
InterCriteria Decision Making Approach to EU Member States Competitiveness Analysis: Trend Analysis ..... 107
Vassia Atanassova, Lyubka Doukovska, Dimitar Karastoyanov, František Čapkovič
Computer-Based Support in Multicriteria Bargaining with Use of the Generalized Raiffa Solution Concept ..... 117
Lech Kruś
Approach to Solve a Criteria Problem of the ABC Algorithm Used to the WBDP Multicriteria Optimization ..... 129
Dawid Ewald, Jacek M. Czerniak, Hubert Zarzycki
Part IV: Issues in Intuitionistic Fuzzy Sets
Representation Theorem of General States on IF-sets ..... 141
Jaroslav Považan
On Finitely Additive IF-States ..... 149
Beloslav Riečan
Embedding of $\boldsymbol{I F}$-States to $\mathbf{M V}$-Algebras ..... 157Beloslav Riečan
Definitive Integral on the Interval of IF Sets ..... 163
Alžbeta Michalíková
Intuitionistic Fuzzy Tautology Definitions for the Validity of Intuitionistic Fuzzy Implications: An Experimental Study ..... 171
Marcin Detyniecki, Marie-Jeanne Lesot, Paul Moncuquet
Short Remark on Fuzzy Sets, Interval Type-2 Fuzzy Sets, General Type-2
Fuzzy Sets and Intuitionistic Fuzzy Sets ..... 183
Oscar Castillo, Patricia Melin, Radoslav Tsvetkov, Krassimir T. Atanassov
Part V: Fuzzy Cognitive Maps and Applications
Integrated Approach for Developing Timed Fuzzy Cognitive Maps ..... 193Evangelia Bourgani, Chrysostomos D. Stylios, George Manis,Voula C. Georgopoulos
Linguistic Approach to Granular Cognitive Maps: User's Tool for Knowledge Accessing and Processing ..... 205
Wtadyslaw Homenda, Witold Pedrycz
Automatic Data Understanding: A Linguistic Tool for Granular Cognitive Maps Designing ..... 217
Władyslaw Homenda, Witold Pedrycz
Part VI: Issues in Logic and Artificial Intelligence
Fixed-Point Methods in Parametric Model Checking ..... 231
Michat Knapik, Wojciech Penczek
Specialized vs. Multi-game Approaches to AI in Games ..... 243Maciej Świechowski, Jacek Mańdziuk
Part VII: Group Decisions, Consensus, Negotiations
Consensus Reaching Processes under Hesitant Linguistic Assessments ..... 257
José Luis García-Lapresta, David Pérez-Román, Edurne Falcó
Consensus Modeling in Multiple Criteria Multi-expert Real Options-Based Valuation of Patents ..... 269
Andrea Barbazza, Mikael Collan, Mario Fedrizzi, Pasi Luukka
Modeling Different Advising Attitudes in a Consensus Focused Process of Group Decision Making ..... 279
Dominika Gotuńska, Janusz Kacprzyk, Enrique Herrera-Viedma
Automated Negotiation with Multi-agent Systems in Business Processes ..... 289Manuella Kadar, Maria Muntean, Adina Cretan, Ricardo Jardim-Gonçalves
Part VIII: Issues in Granular Computing
Extended Index Matrices ..... 305
Krassimir T. Atanassov
Some Remarks on the Fuzzy Linguistic Model Based on Discrete Fuzzy Numbers ..... 319
Enrique Herrera-Viedma, Juan Vicente Riera, Sebastià Massanet, Joan Torrens
Differences between Moore and RDM Interval Arithmetic ..... 331
Marek Landowski
Interval-Valued Fuzzy Preference Relations and Their Properties ..... 341Urszula Bentkowska
Combining Uncertainty and Vagueness in Time Intervals ..... 353
Christophe Billiet, Guy De Tré
Equality in Approximate Tolerance Geometry ..... 365
Gwendolin Wilke
Estimators of the Relations of: Equivalence, Tolerance and Preference on the Basis of Pairwise Comparisons with Random Errors ..... 377
Leszek Klukowski
Part IX: Multiagent Systems
An Intelligent Architecture for Autonomous Virtual Agents Inspired by Onboard Autonomy ..... 391
Kaveh Hassani, Won-Sook Lee
A Decentralized Multi-agent Approach to Job Scheduling in Cloud Environment ..... 403
Jakub Gqsior, Franciszek Seredyński
Model Checking Properties of Multi-agent Systems with Imperfect Information and Imperfect Recall ..... 415
Jerzy Pilecki, Marek A. Bednarczyk, Wojciech Jamroga
AjTempura - First Software Prototype of C3A Model ..... 427
Vladimir Valkanov, Asya Stoyanova-Doycheva, Emil Doychev, Stanimir Stoyanov, Ivan Popchev, Irina Radeva
Part X: Metaheuristics and Applications
A Neutral Mutation Operator in Grammatical Evolution ..... 439
Christian Oesch, Dietmar Maringer
Study of Flower Pollination Algorithm for Continuous Optimization ..... 451
Szymon Łukasik, Piotr A. Kowalski
Search Space Reduction in the Combinatorial Multi-agent Genetic Algorithms ..... 461
Łukasz Chomatek, Danuta Zakrzewska
Experimental Study of Selected Parameters of the Krill Herd Algorithm ..... 473
Piotr A. Kowalski, Szymon Łukasik
Hybrid Cuckoo Search-Based Algorithms for Business Process Mining ..... 487Viorica R. Chifu, Cristina Bianca Pop, Ioan Salomie, Emil St. Chifu,Victor Rad, Marcel Antal
Direct Particle Swarm Repetitive Controller with Time-Distributed Calculations for Real Time Implementation ..... 499
Piotr Biernat, Bartlomiej Ufnalski, Lech M. Grzesiak
Artificial Fish Swarm Algorithm for Energy-Efficient Routing Technique ..... 509
Asmaa Osama Helmy, Shaimaa Ahmed, Aboul Ella Hassenian
Part XI: Issues in Data Analysis and Data Mining
An Intelligent Flexible Querying Approach for Temporal Databases ..... 523
Aymen Gammoudi, Allel Hadjali, Boutheina Ben Yaghlane
Effective Outlier Detection Technique with Adaptive Choice of Input Parameters ..... 535
Agnieszka Duraj, Danuta Zakrzewska
Data Quality Improvement by Constrained Splitting ..... 547
Antoon Bronselaer, Guy De Tré
Auditing-as-a-Service for Cloud Storage ..... 559
Alshaimaa Abo-alian, N.L. Badr, M.F. Tolba
Data Driven XPath Generation ..... 569Robin De Mol, Antoon Bronselaer, Joachim Nielandt, Guy De Tré
Selection of Semantical Mapping of Attribute Values for Data Integration ..... 581
Marcin Szymczak, Antoon Bronselaer, Stawomir Zadrożny, Guy De Tré
A Knowledge-Driven Tool for Automatic Activity Dataset Annotation ..... 593
Gorka Azkune, Aitor Almeida, Diego López-de-Ipiña, Liming Chen
Multimodal Statement Networks for Organic Rankine Cycle Diagnostics - Use Case of Diagnostic Modeling ..... 605
Tomasz Rogala, Marcin Amarowicz
Gradual Forgetting Operator in Intuitionistic Statement Networks ..... 613
Wojciech Cholewa
Part XII: Issues in Generalized Nets
A Generalized Net Model Based on Fast Learning Algorithm of Unsupervised Art2 Neural Network ..... 623
Todor Petkov, Sotir Sotirov
Intuitionistic Fuzzy Evaluation of the Behavior of Tokens in Generalized Nets ..... 633
Velin Andonov, Anthony Shannon
Generalized Net Description of Essential Attributes Generator in SEAA Method ..... 645
Maciej Krawczak, Grażyna Szkatuła
Development of Generalized Net for Testing of Different Mathematical Models of E. coli Cultivation Process ..... 657
Dimitar Dimitrov, Olympia Roeva
Part XIII: Neural Networks, Modeling and Learning
An Approach to RBF Initialization with Feature Selection ..... 671
Ireneusz Czarnowski, Piotr Jędrzejowicz
Artificial Neural Network Ensembles in Hybrid Modelling of Activated Sludge Plant ..... 683
Jukka Keskitalo, Kauko Leiviskä
Implicit GPC Based on Semi Fuzzy Neural Network Model ..... 695Margarita Terziyska, Lyubka Doukovska, Michail Petrov
Comparison of Neural Networks with Different Membership Functions in the Type-2 Fuzzy Weights ..... 707
Fernando Gaxiola, Patricia Melin, Fevrier Valdez
Multi-dimensional Fuzzy Modeling with Incomplete Fuzzy Rule Base and Radial Basis Activation Functions ..... 715
Gancho Vachkov, Nikolinka Christova, Magdalena Valova
Application of Artificial Neural Networks for Modelling of Nicolsky- Eisenman Equation and Determination of Ion Activities in Mixtures . ..... 727
Józef Wiora, Dariusz Grabowski, Alicja Wiora, Andrzej Kozyra
Part XIV: Classification and Clustering
An Interval-Valued Fuzzy Classifier Based on an Uncertainty-Aware Similarity Measure ..... 741
Anna Stachowiak, Patryk Żywica, Krzysztof Dyczkowski, Andrzej Wójtowicz
Differential Evolution Based Nearest Prototype Classifier with Optimized Distance Measures and GOWA ..... 753
David Koloseni, Pasi Luukka
Differential Evolution Classifier with Optimized OWA-Based Multi-distance Measures for the Features in the Data Sets ..... 765
David Koloseni, Mario Fedrizzi, Pasi Luukka, Jouni Lampinen, Mikael Collan
Intuitionistic Fuzzy Decision Tree: A New Classifier ..... 779
Pawet Bujnowski, Eulalia Szmidt, Janusz Kacprzyk
Characterization of Large Target Sets with Probabilistic Classifiers ..... 791Ray-Ming Chen
Data-Based Approximation of Fuzzy Target Sets ..... 801
Ray-Ming Chen
Part XV: Perception, Judgment, Affect, and Sentiment Analyses
Towards Perception-Oriented Situation Awareness Systems ..... 813
Gianpio Benincasa, Giuseppe D'Aniello, Carmen De Maio, Vincenzo Loia, Francesco Orciuoli
Textual Event Detection Using Fuzzy Fingerprints ..... 825
Luís Marujo, Joao Paulo Carvalho, Anatole Gershman, Jaime Carbonell, João P. Neto, David Martins de Matos
Inferring Drivers Behavior through Trajectory Analysis ..... 837Eduardo M. Carboni, Vania Bogorny
Framework for Customers' Sentiment Analysis ..... 849Catarina Marques-Lucena, João Sarraipa, Joaquim Fonseca, António Grilo,Ricardo Jardim-Gonçalves
Author Index ..... 861

# InterCriteria Decision Making Approach to EU Member States Competitiveness Analysis: Temporal and Threshold Analysis 

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#### Abstract

In this paper, we present some interesting findings from the application of our recently developed InterCriteria Decision Making (ICDM) approach to data extracted from the World Economic Forum's Global Competitiveness Reports for the years 2008-2009 to 2013-2014 for the current 28 Member States of the European Union. The developed approach which employs the apparatuses of index matrices and intuitionistic fuzzy sets is designed to produce from an existing index matrix with multiobject multicriteria evaluations a new index matrix that contains intuitionistic fuzzy pairs with the correlations revealed to exist in between the set of evaluation criteria, which are not obligatory there 'by design' of the WEF's methodology but exist due to the integral, organic nature of economic data. Here, we analyse the data from the six-year period within a reasonably chosen intervals for the thresholds of the intuitionistic fuzzy functions of membership and non-membership, and make a series of observations about the current trends in the factors of competitiveness of the European Union. The whole research and the conclusions derived are in line with WEF's address to state policy makers to identify and strengthen the transformative forces that will drive future economic growth.


Keywords: Global Competitiveness Index, Index matrix, InterCriteria decision making, Intuitionistic fuzzy sets, Multicriteria decision making.

## 1 Introduction

The present work contains a continuation of our recent research, started in [7], which aims at analyzing data about the performance of the 28 European Union Member

States according to the Global Competitiveness Reports (GCRs) of the World Economic Forum (WEF), released in the period from 2008-2009 to 2013-2014. We use a recently developed multicriteria decision making method, based on intuitionistic fuzzy sets and index matrices, two mathematical formalisms proposed and significantly researched by Atanassov in a series of publications from 1980s to present day. As its title, InterCriteria Decision Making (ICDM, see [6]), suggests, the method aims at discovery of existing dependences between the evaluation criteria themselves.

The ICDM approach has been originally devised to reflect situations where some of the criteria come at a higher cost than others, for instance are harder, more expensive and/or more time consuming to measure or evaluate. Such criteria are generally considered unfavourable, hence if the method identifies certain level of correlation between such unfavourable criteria and others that are easier, cheaper or quicker to measure or evaluate, the unfavourable ones might be disregarded in the further decision making process.

In our work for applying ICDM to WEF GCR data [7] we have been interested to detect the eventual correlations between the 12 'pillars of country competitiveness', in order to outline fewer pillars on which policy makers should concentrate their efforts. Our motivation to conduct the analysis has been that it might be expected that improved country's performance against some pillars would positively affect the country's performance in the respective correlating ones. This is in line with WEF's address to state policy makers to identify and strengthen the transformative forces that will drive future economic growth of the countries, as formulated in the Preface of the latest Global Competitiveness Report 2013-2014, [8].

The twelve pillars in the WEF's methodology are grouped in three subindices:

- The first subindex 'Basic requirements' contains pillars 1-4: '1. Institutions', '2. Infrastructure', '3. Macroeconomic stability' and '4. Health and primary education', $25 \%$ weight for each pillar.
- The second subindex 'Efficiency enhancers' contains pillars 5-10: '5. Higher education and training', ' 6 . Goods market efficiency', '7. Labor market efficiency’, '8. Financial market sophistication', '9. Technological readiness' and '10. Market size', $17 \%$ weight for each pillar.
- The third subindex 'Innovation and sophistication factors' contains pillars 11-12: ' 11 . Business sophistication' and ' 12 . Innovation', $50 \%$ weight for each pillar.

On the basis of the evaluation of the countries according to these pillars and following a sophisticated methodology, WEF determines their 'stage of development', which is one of the five possible alternatives: ' 1 . Factor driven', 'Transition 1-2', '2. Efficiency driven', 'Transition 2-3' or '3. Innovation driven'. From the 28 EU Member States, 19 are in stage ' 3 . Innovation driven', 7 are in stage 'Transition 2-3', and 2 are in stage ' 2 . Efficiency driven'.

In the first part of our research [7], we gave the comparison of the results of the ICDM for the two extreme years in the 6-year period, and discussed in more details the findings for the year 2013-2014. We showed the principle of gradual discovery of more correlations between the criteria by letting the two user defined thresholds involved in the ICDM approach change within the [0;1]-interval. Example was given
with a detailed description of the correlations in one partial case, and it was visually interpreted as a graph. Here, we will continue investigating the same selection of data, but we will further show how for each year, and for each pair of thresholds, the number of positive consonances for each of the twelve pillars change, and will accompany these observations with some initial conclusions.

This paper is organized as follows. In Section 2 the two basic mathematical concepts that we use - intuitionistic fuzzy sets and index matrices - are briefly presented and on this basis is described, the proposed method ICDM. Section 3 contains our results from applying the method to analysis of a selection of data about the performance of the currently 28 Member States of the EU during the last six years against the twelve pillars of competitiveness. We report the findings of our temporal and threshold analysis, and formulate our conclusions in the last Section 4.

## 2 Basic Concepts and Method

The presented multicriteria decision making method is based on two fundamental concepts: intuitionistic fuzzy sets and index matrices.

Intuitionistic fuzzy sets defined by Atanassov (cf. [1, 2, 4, 5]) represent an extension of the concept of fuzzy sets, as defined by Zadeh [9], exhibiting function $\mu_{A}(x)$ defining the membership of an element $x$ to the set $A$, evaluated in the [0;1]-interval. The difference between fuzzy sets and intuitionistic fuzzy sets (IFSs) is in the presence of a second function $v_{A}(x)$ defining the non-membership of the element $x$ to the set $A$, where $\mu_{A}(x) \in[0 ; 1], v_{A}(x) \in[0 ; 1]$, and moreover $\left(\mu_{A}(x)+v_{A}(x)\right) \in[0 ; 1]$.

The IFS itself is formally denoted by:

$$
A=\left\{\left\langle x, \mu_{A}(x), v_{A}(x)\right\rangle \mid x \in E\right\}
$$

Comparison between elements of any two IFSs, say $A$ and $B$, involves pairwise comparisons between their respective elements' degrees of membership and nonmembership to both sets.

The second concept on which the proposed method relies is the concept of index matrix, a matrix which features two index sets. The theory behind the index matrices is described in [3]. Here we will start with the index matrix $M$ with index sets with $m$ rows $\left\{C_{1}, \ldots, C_{m}\right\}$ and $n$ columns $\left\{O_{1}, \ldots, O_{n}\right\}$ :

$$
M=\begin{array}{r|ccccccc} 
& O_{1} & \ldots & O_{k} & \ldots & O_{l} & \ldots & O_{n} \\
\hline C_{1} & a_{C_{1}, O_{1}} & \ldots & a_{C_{1}, O_{k}} & \ldots & a_{C_{1}, o_{l}} & \ldots & a_{C_{1}, O_{n}} \\
\vdots & \vdots & \ddots & \vdots & \ddots & \vdots & \ddots & \vdots \\
C_{i} & a_{C_{i}, O_{1}} & \ldots & a_{C_{i}, O_{k}} & \ldots & a_{C_{i}, O_{l}} & \ldots & a_{C_{i}, O_{n}} \\
\vdots & \vdots & \ddots & \vdots & \ddots & \vdots & \ddots & \vdots \\
C_{j} & a_{C_{j}, O_{1}} & \ldots & a_{C_{j}, O_{k}} & \ldots & a_{C_{j}, O_{l}} & \ldots & a_{C_{j}, O_{n}} \\
\vdots & \vdots & \ddots & \vdots & \ddots & \vdots & \ddots & \vdots \\
C_{m} & a_{C_{m}, O_{1}} & \ldots & a_{C_{m}, O_{j}} & \ldots & a_{C_{m}, o_{l}} & \ldots & a_{C_{m}, O_{n}}
\end{array}
$$

where for every $p, q(1 \leq p \leq m, 1 \leq q \leq n), C_{p}$ is a criterion (in our case, one of the twelve pillars), $O_{q}$ in an evaluated object (in our case, one of the 28 EU Member states), $a_{C_{p} o_{q}}$ is the evaluation of the $q$-th object against the $p$-th criterion, and it is defined as a real number or another object that is comparable according to relation $R$ with all the rest elements of the index matrix $M$, so that for each $i, j, k$ it holds the relation $R\left(a_{C_{k} O_{i}}, a_{C_{k} O_{j}}\right)$. The relation R has dual relation $\bar{R}$, which is true in the cases when relation $R$ is false, and vice versa.

For the needs of our decision making method, pairwise comparisons between every two different criteria are made along all evaluated objects. During the comparison, it is maintained one counter of the number of times when the relation $R$ holds, and another counter for the dual relation.

Let $S_{k, l}^{\mu}$ be the number of cases where the relations $R\left(a_{C_{k} O_{i}}, a_{C_{k} O_{j}}\right)$ and $R\left(a_{C_{I} O_{i}}, a_{C_{O} O_{j}}\right)$ are simultaneously satisfied. Let also $S_{k, l}^{v}$ be the number of cases in which the relations $R\left(a_{C_{k} O_{i}}, a_{C_{k} O_{j}}\right)$ and its dual $\bar{R}\left(a_{C_{l} O_{i}}, a_{C_{l} O_{j}}\right)$ are simultaneously satisfied. As the total number of pairwise comparisons between the object is $n(n-1) / 2$, it is seen that there hold the inequalities:

$$
0 \leq S_{k, l}^{\mu}+S_{k, l}^{v} \leq \frac{n(n-1)}{2} .
$$

For every $k, l$, such that $1 \leq k \leq l \leq m$, and for $n \geq 2$ two numbers are defined:

$$
\mu_{C_{k}, C_{l}}=2 \frac{S_{k, l}^{\mu}}{n(n-1)}, v_{C_{k}, C_{l}}=2 \frac{S_{k, l}^{V}}{n(n-1)} .
$$

The pair constructed from these two numbers plays the role of the intuitionistic fuzzy evaluation of the relations that can be established between any two criteria $C_{k}$ and $C_{l}$. In this way the index matrix $M$ that relates evaluated objects with evaluating criteria can be transformed to another index matrix $M^{*}$ that gives the relations among the criteria:

$$
M^{*}=\begin{array}{c|ccc}
C_{1} & C_{1} & \ldots & C_{m} \\
\vdots & \left\langle\mu_{C_{1}, C_{1}}, v_{C_{1}, C_{1}}\right\rangle & \ldots & \left\langle\mu_{C_{1}, C_{m}}, v_{C_{1}, C_{m}}\right\rangle \\
\vdots & \vdots & \ddots & \vdots \\
C_{m} & \left\langle\mu_{C_{m}, C_{1},}, v_{C_{1}, C_{m}}\right\rangle & \ldots & \left\langle\mu_{C_{m}, C_{m},}, v_{C_{m}, C_{m}}\right\rangle
\end{array} .
$$

The final step of the algorithm is to determine the degrees of correlation between the criteria, depending on the user's choice of $\mu$ and $\nu$. We call these correlations between the criteria: 'positive consonance', 'negative consonance' or 'dissonance'.

Let $\alpha, \beta \in[0 ; 1]$ be given, so that $\alpha+\beta \leq 1$. We say that criteria $C_{k}$ and $C_{l}$ are in:

- $(\alpha, \beta)$-positive consonance, if $\mu_{C_{k}, C_{l}}>\alpha$ and $v_{C_{k}, C_{l}}<\beta$;
- $(\alpha, \beta)$-negative consonance, if $\mu_{C_{k}, C_{l}}<\beta$ and $v_{C_{k} C_{l}}>\alpha$;
- $(\alpha, \beta)$-dissonance, otherwise.

Obviously, the larger $\alpha$ and/or the smaller $\beta$, the less number of criteria may be simultaneously connected with the relation of ( $\alpha, \beta$ )-positive consonance. For practical purposes, it carries the most information when either the positive or the negative consonance is as large as possible, while the cases of dissonance are less informative and are skipped.

## 3 Main Results

We ran the described algorithm over a selection of data from last six WEF GCRs for the 28 (present) EU Member States from the period 2008-2009 to 2013-2014. The algorithm, as described in Section 2, produces the results with precision of 9 digits after the decimal point, however, we will use here precision of only 3 digits. From the six index matrices of data for 28 countries evaluated according to 12 pillars, we obtain six index matrices $12 \times 12$ for the intuitionistic fuzzy $\mu$-function and six more index matrices $12 \times 12$ for the intuitionistic fuzzy $v$-function. Obviously, in the first IM, along the main diagonal, $\mu_{C_{k}, C_{k}}=1$, while in the second IM, along the main diagonal, $v_{C_{k}, C_{k}}=0$, because naturally every pillar is in perfect positive consonance to itself. The sum of the values of the respective elements of the two IMs is generally:

$$
0 \leq \mu_{C_{k}, C_{l}}+v_{C_{k}, C_{l}} \leq 1
$$

though in most cases it should be expected that this non-strict inequality is practically a strict one ( $0 \leq \mu_{C_{k}, C_{l}}+v_{C_{k}, C_{l}}<1$ ), thus leaving room for the complement to 1 , that gives the measure of uncertainty.

Our aim will be to study how the positive consonance pairs of pillars behave over the considered 6 -year period and for different runs of the values of the thresholds $\alpha, \beta$. We focus on the positive consonances, although in a separate leg of research it might prove useful to focus on the negative ones, too. The study goes in two directions:

- how within a fixed year, changing the thresholds $\alpha, \beta$ changes the number of consonances formed for each of the twelve pillars, and
- how for a fixed pair of values of $\alpha, \beta$ these consonances change over time.

To start with, we will repeat from [7] the two $12 \times 12$ index matrices with the revealed intercriteria relations. Table 1 below gives the values of the intuitionistic fuzzy $\mu$-function, and Table 2 gives the values of the intuitionistic fuzzy $v$-function. Here, all cells are coloured in the greyscale, with the highest values coloured in the darkest shade of grey, while the lowest ones are coloured in white. Of course, every criteria perfectly correlates with itself, so for any $i$ the value $\mu_{C_{i} C_{i}}=1$, and $v_{C_{i} C_{i}}=\pi_{C_{i} C_{i}}=0$. Also, the matrices are obviously symmetrical according to the main diagonals.

Table 1. Comparison of the calculated values of $\mu_{C_{i} C_{j}}$ for years 2008-2009 and 2013-2014


Table 2. Comparison of the calculated values of $v_{C_{i} C_{j}}$ for years 2008-2009 and 2013-2014


Case 1. Fixed years, changing thresholds $\alpha, \beta$
In Tables $3-8$, where $\alpha, \beta$ run from $(0.7 ; 0.3)$ to $(0.85 ; 0.15)$, for each pillar is given the number of the rest pillars, which it is in positive consonance with, as evaluated by $\mu_{C_{k}, C_{l}}>\alpha$ and $v_{C_{k}, c_{l}}<\beta$. We will note that we skip the columns for pillars '3. Macroeconomic stability' and '10. Market size', since both do not enter into positive consonance with any of the rest.

Table 3. Results for fixed year 2008-2009.

| $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 0.825 | 0.175 | 3 | 2 | 0 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 5 | 6 |
| 0.8 | 0.2 | 5 | 3 | 0 | 0 | 3 | 0 | 3 | 5 | 3 | 4 | 13 | 7 |
| 0.775 | 0.225 | 7 | 4 | 1 | 3 | 4 | 0 | 3 | 6 | 5 | 5 | 19 | 9 |
| 0.75 | 0.25 | 8 | 8 | 5 | 7 | 6 | 0 | 4 | 7 | 7 | 8 | 30 | 9 |
| 0.725 | 0.275 | 8 | 8 | 5 | 8 | 7 | 0 | 7 | 7 | 8 | 8 | 33 | 9 |
| 0.7 | 0.3 | 8 | 8 | 8 | 8 | 8 | 0 | 8 | 8 | 8 | 8 | 36 | 9 |

Table 4. Results for fixed year 2009-2010.

| $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 0.825 | 0.175 | 2 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 1 | 1 | 4 | 5 |
| 0.8 | 0.2 | 3 | 1 | 0 | 1 | 2 | 0 | 0 | 3 | 1 | 5 | 8 | 7 |
| 0.775 | 0.225 | 7 | 4 | 3 | 3 | 5 | 0 | 2 | 5 | 6 | 7 | 21 | 9 |
| 0.75 | 0.25 | 8 | 4 | 4 | 5 | 6 | 0 | 2 | 5 | 7 | 7 | 24 | 9 |
| 0.725 | 0.275 | 8 | 5 | 5 | 6 | 8 | 0 | 3 | 7 | 7 | 7 | 28 | 9 |
| 0.7 | 0.3 | 8 | 7 | 8 | 8 | 8 | 0 | 6 | 8 | 7 | 8 | 34 | 9 |

Table 5. Results for fixed year 2010-2011.

| $\boldsymbol{1} \boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 0}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| 0.825 | 0.175 | 3 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 2 | 4 | 5 |
| 0.8 | 0.2 | 5 | 2 | 0 | 2 | 1 | 0 | 0 | 2 | 3 | 5 | 10 | 7 |
| 0.775 | 0.225 | 5 | 3 | 0 | 2 | 4 | 0 | 0 | 5 | 5 | 6 | 15 | 7 |
| 0.75 | 0.25 | 6 | 4 | 1 | 3 | 5 | 0 | 0 | 5 | 6 | 6 | 18 | 8 |
| 0.725 | 0.275 | 6 | 4 | 3 | 5 | 6 | 0 | 0 | 6 | 7 | 7 | 22 | 8 |
| 0.7 | 0.3 | 8 | 5 | 5 | 7 | 7 | 0 | 2 | 6 | 7 | 7 | 27 | 9 |

Table 6. Results for fixed year 2011-2012.

| $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 2 | 3 |
| 0.825 | 0.175 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 3 | 3 | 3 | 6 | 5 |
| 0.8 | 0.2 | 3 | 3 | 0 | 1 | 0 | 0 | 0 | 4 | 4 | 5 | 10 | 6 |
| 0.775 | 0.225 | 5 | 3 | 0 | 3 | 2 | 0 | 0 | 5 | 5 | 5 | 14 | 7 |
| 0.75 | 0.25 | 5 | 3 | 0 | 4 | 3 | 0 | 0 | 6 | 6 | 5 | 16 | 7 |
| 0.725 | 0.275 | 7 | 4 | 0 | 4 | 5 | 0 | 2 | 6 | 6 | 6 | 20 | 8 |
| 0.7 | 0.3 | 7 | 5 | 1 | 6 | 7 | 1 | 3 | 7 | 7 | 6 | 25 | 10 |

Table 7. Results for fixed year 2012-2013.

| $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 2 | 3 |
| 0.825 | 0.175 | 3 | 0 | 0 | 0 | 1 | 0 | 0 | 3 | 2 | 4 | 7 | 5 |
| 0.8 | 0.2 | 5 | 1 | 0 | 2 | 2 | 0 | 0 | 4 | 4 | 4 | 11 | 7 |
| 0.775 | 0.225 | 5 | 3 | 0 | 4 | 2 | 0 | 0 | 6 | 5 | 5 | 15 | 7 |
| 0.75 | 0.25 | 5 | 3 | 0 | 4 | 3 | 0 | 0 | 6 | 6 | 5 | 16 | 7 |
| 0.725 | 0.275 | 8 | 5 | 1 | 7 | 6 | 2 | 3 | 6 | 6 | 6 | 25 | 10 |
| 0.7 | 0.3 | 9 | 5 | 6 | 7 | 8 | 3 | 4 | 8 | 7 | 7 | 32 | 10 |

Table 8. Results for fixed year 2013-2014.

| $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.85 | 0.15 | 3 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 3 | 5 | 6 |
| 0.825 | 0.175 | 3 | 0 | 0 | 1 | 1 | 0 | 0 | 2 | 1 | 4 | 6 | 6 |
| 0.8 | 0.2 | 5 | 1 | 0 | 3 | 1 | 0 | 0 | 3 | 5 | 4 | 11 | 7 |
| 0.775 | 0.225 | 5 | 3 | 0 | 4 | 2 | 0 | 0 | 6 | 5 | 5 | 15 | 7 |
| 0.75 | 0.25 | 5 | 3 | 0 | 4 | 4 | 0 | 0 | 6 | 6 | 6 | 17 | 7 |
| 0.725 | 0.275 | 8 | 4 | 1 | 7 | 6 | 0 | 2 | 6 | 6 | 6 | 23 | 9 |
| 0.7 | 0.3 | 9 | 5 | 3 | 7 | 7 | 4 | 3 | 7 | 7 | 6 | 29 | 10 |

From the data in Tables 3-8, we can make some general observations concerning the thresholds $\alpha, \beta$. These observations are needed for setting the general framework in which the findings of the present research can be usefully interpreted. Obviously, neither too few, nor too many correlating pillars would help yield an effective economic analysis.

- Observation 1. Three of the twelve pillars, namely, the basic requirement pillar '3. Macroeconomic stability' and the efficiency enhancer pillars '7. Labor market efficiency' and ' 10 . Market size' tend to avoid positive consonances with the rest pillars in the WEF GCR methodology, which is especially well expressed for the $3^{\text {rd }}$ and $10^{\text {th }}$ pillars (for all studied years, the values of $\mu_{C_{3}, C_{l}}$ ranging from 0.648 to 0.693 and the maximal value of $\mu_{C_{10}, C_{l}}$ ranging from 0.622 to 0.672 ). In general, it is worth analysing to what extent it is natural to have these pillars uncorrelated to the rest, or to what extent it results from particular governments' malperformance.
- Observation 2. Under a certain value for threshold $\alpha$ (respectively, above a certain value for threshold $\beta$ ), it is natural that all pillars start correlating, which is ineffective for the analysis. In the light of the Observation 1, we can safely focus only on the thresholds when the 9 out of 12 pillars start correlating, which is at $\alpha=0.775$ for the first two years, and with $\alpha$ falling to around 0.725 in the next four years. Hence, it is interesting to analyse the data corresponding to larger values of threshold $\alpha$.
- Observation 3. In the other extreme, analysing data for too few pillars being in positive consonance is not effective either. We observe that until 2013-2014, the number of unique correlating pillars when $\alpha=0.85$ is 2 or 3 out of 12 (mainly ' 11 . Business sophistication' and '12. Innovation', sometimes accompanied by the basic requirement pillar ' 1 . Institutions'). The sudden number of six correlating pillars with as high threshold for $\alpha$ as 0.85 can be interpreted as a sign of raising mutual dependence of the different aspects of competitiveness, yet observations for next periods are needed for a more categorical conclusion.

Hence, it is most useful to focus the analysis in the range from $(0.775 ; 0.225)$ to ( $0.825 ; 0.175$ ). Besides the more general observations about the thresholds, we can also make some more specific observations about the pillars.

- Observation 4. The efficiency enhancer pillar '7. Labor market efficiency' starts correlating with the rest pillars only after year 2011-2012, and only in the low values of $\alpha$ from 0.7 to 0.75 .
- Observation 5. The efficiency enhancer pillar '8. Financial market sophistication' in 2008-2009 and 2009-2010 was in consonance with other pillars as of $\alpha=0.825$ or 0.775 , respectively, after the $\alpha$ threshold for the $8^{\text {th }}$ pillar falls down to $\alpha=0.725$ and even 0.7 , meaning that it becomes much weakly correlated.
- Observation 6. Pillars '11. Business sophistication' and '12. Innovation' have shown the greatest and most stable positive consonance between each other, as well as with the other pillars. This is not surprising, given that both pillars form with $50 \%$ weight each the third subindex 'Innovation and sophistication factors'.

Case 2. Fixed thresholds $\alpha, \beta$, changing years
In the following temporal analysis (Tables 9-15) we compare how the pillars have correlated for the last six years at fixed values of the thresholds $\alpha, \beta$.

Table 9. Results for fixed year $\alpha=0.85, \beta=0.15$.

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| $2009-2010$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| $2010-2011$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 |
| $2011-2012$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 2 | 3 |
| $2012-2013$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 2 | 3 |
| $2013-2014$ | 3 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 3 | 5 | 6 |

Table 10. Results for fixed year $\alpha=0.825, \beta=0.175$.

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 3 | 2 | 0 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 5 | 6 |
| $2009-2010$ | 2 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 1 | 1 | 4 | 5 |
| $2010-2011$ | 3 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 2 | 4 | 5 |
| $2011-2012$ | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 3 | 3 | 3 | 6 | 5 |
| $2012-2013$ | 3 | 0 | 0 | 0 | 1 | 0 | 0 | 3 | 2 | 4 | 7 | 5 |
| $2013-2014$ | 3 | 0 | 0 | 1 | 1 | 0 | 0 | 2 | 1 | 4 | 6 | 6 |

Table 11. Results for fixed year $\alpha=0.8, \beta=0.2$.

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 5 | 3 | 0 | 0 | 3 | 0 | 3 | 5 | 3 | 4 | 13 | 7 |
| $2009-2010$ | 3 | 1 | 0 | 1 | 2 | 0 | 0 | 3 | 1 | 5 | 8 | 7 |
| $2010-2011$ | 5 | 2 | 0 | 2 | 1 | 0 | 0 | 2 | 3 | 5 | 10 | 7 |
| $2011-2012$ | 3 | 3 | 0 | 1 | 0 | 0 | 0 | 4 | 4 | 5 | 10 | 6 |
| $2012-2013$ | 5 | 1 | 0 | 2 | 2 | 0 | 0 | 4 | 4 | 4 | 11 | 7 |
| $2013-2014$ | 5 | 1 | 0 | 3 | 1 | 0 | 0 | 3 | 5 | 4 | 11 | 7 |

Table 12. Results for fixed year $\alpha=0.775, \beta=0.225$.

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 7 | 4 | 1 | 3 | 4 | 0 | 3 | 6 | 5 | 5 | 19 | 9 |
| $2009-2010$ | 7 | 4 | 3 | 3 | 5 | 0 | 2 | 5 | 6 | 7 | 21 | 9 |
| $2010-2011$ | 5 | 3 | 0 | 2 | 4 | 0 | 0 | 5 | 5 | 6 | 15 | 7 |
| $2011-2012$ | 5 | 3 | 0 | 3 | 2 | 0 | 0 | 5 | 5 | 5 | 14 | 7 |
| $2012-2013$ | 5 | 3 | 0 | 4 | 2 | 0 | 0 | 6 | 5 | 5 | 15 | 7 |
| $2013-2014$ | 5 | 3 | 0 | 4 | 2 | 0 | 0 | 6 | 5 | 5 | 15 | 7 |

Table 13. Results for fixed year $\alpha=0.75, \beta=0.25$

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 8 | 8 | 5 | 7 | 6 | 0 | 4 | 7 | 7 | 8 | 30 | 9 |
| $2009-2010$ | 8 | 4 | 4 | 5 | 6 | 0 | 2 | 5 | 7 | 7 | 24 | 9 |
| $2010-2011$ | 6 | 4 | 1 | 3 | 5 | 0 | 0 | 5 | 6 | 6 | 18 | 8 |
| $2011-2012$ | 5 | 3 | 0 | 4 | 3 | 0 | 0 | 6 | 6 | 5 | 16 | 7 |
| $2012-2013$ | 5 | 3 | 0 | 4 | 3 | 0 | 0 | 6 | 6 | 5 | 16 | 7 |
| $2013-2014$ | 5 | 3 | 0 | 4 | 4 | 0 | 0 | 6 | 6 | 6 | 17 | 7 |

Table 14. Results for fixed year $\alpha=0.725, \beta=0.275$

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 8 | 8 | 5 | 8 | 7 | 0 | 7 | 7 | 8 | 8 | 33 | 9 |
| $2009-2010$ | 8 | 5 | 5 | 6 | 8 | 0 | 3 | 7 | 7 | 7 | 28 | 9 |
| $2010-2011$ | 6 | 4 | 3 | 5 | 6 | 0 | 0 | 6 | 7 | 7 | 22 | 8 |
| $2011-2012$ | 7 | 4 | 0 | 4 | 5 | 0 | 2 | 6 | 6 | 6 | 20 | 8 |
| $2012-2013$ | 8 | 5 | 1 | 7 | 6 | 2 | 3 | 6 | 6 | 6 | 25 | 10 |
| $2013-2014$ | 8 | 4 | 1 | 7 | 6 | 0 | 2 | 6 | 6 | 6 | 23 | 9 |

Table 15. Results for fixed year $\alpha=0.7, \beta=0.3$

| Year | $\boldsymbol{C}_{\mathbf{1}}$ | $\boldsymbol{C}_{\mathbf{2}}$ | $\boldsymbol{C}_{\mathbf{4}}$ | $\boldsymbol{C}_{\mathbf{5}}$ | $\boldsymbol{C}_{\mathbf{6}}$ | $\boldsymbol{C}_{\mathbf{7}}$ | $\boldsymbol{C}_{\mathbf{8}}$ | $\boldsymbol{C}_{\mathbf{9}}$ | $\boldsymbol{C}_{\mathbf{1 1}}$ | $\boldsymbol{C}_{\mathbf{1 2}}$ | Rel | Uniq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2008-2009$ | 8 | 8 | 8 | 8 | 8 | 0 | 8 | 8 | 8 | 8 | 36 | 9 |
| $2009-2010$ | 8 | 7 | 8 | 8 | 8 | 0 | 6 | 8 | 7 | 8 | 34 | 9 |
| $2010-2011$ | 8 | 5 | 5 | 7 | 7 | 0 | 2 | 6 | 7 | 7 | 27 | 9 |
| $2011-2012$ | 7 | 5 | 1 | 6 | 7 | 1 | 3 | 7 | 7 | 6 | 25 | 10 |
| $2012-2013$ | 9 | 5 | 6 | 7 | 8 | 3 | 4 | 8 | 7 | 7 | 32 | 10 |
| $2013-2014$ | 9 | 5 | 3 | 7 | 7 | 4 | 3 | 7 | 7 | 6 | 29 | 10 |

- Observation 7. We can observe that as of $\alpha=0.85$, pillars 11 and 12 are again sustainably correlating during the whole period, and as of $\alpha=0.825$ the basic requirement pillar ' 1 . Institutions' also tends to enter in positive consonances, i.e. it is a factor of significant importance for the rest competitiveness pillars.
- Observation 8. With less but also visible importance are the efficiency enhancer pillars '9. Technological readiness' and ' 6 . Goods market efficiency'.
- Observation 9. With $(\alpha ; \beta)$ starting from $(0.8 ; 0.2)$ down to $(0.7 ; 0.3)$, we note that the number of positive consonances of the basic requirement pillar ' 2 . Infrastructure' gradually reduces in time.
- Observation 10. We can also note that with the relatively high $\alpha>0.75$, the efficiency enhancer pillar '8. Financial market sophistication' has been in positive consonances only in the period 2008-2010, and for smaller $\alpha$ it has been visibly less correlated after 2010, than it was before.
- Observation 11. A very similar to observation to the previous one can also be made for the basic requirement pillar '4. Health and primary education'. Compared to it, the efficiency enhancer pillar '5. Higher education and training' naturally shows higher levels of positive consonance with the rest competitiveness pillars for different runs of $(\alpha ; \beta)$ throughout the whole period.
- Observation 12. The efficiency enhancer pillar '7. Labor market efficiency' has only started exhibiting for $\alpha>0.75$ and only in the last year.

Beyond these observations, a more detailed and profound analysis of these data should be done by economists, taking into consideration various factors like the beginning of the world financial crisis, accession of new Member States to the European Union, certain changes in legislation, technological breakthroughs. It is also worth noting that in some pillars, like '4. Health and primary education' and '5. Higher education and training' effects should only be expected to occur after certain periods of time, which makes it necessary to continue the present research.

## 4 Conclusions

With the present temporal and threshold analysis of the WEF's Global Competitiveness Reports data for the EU Member States, we aim to continue and further elaborate on our analysis of the revealed relations between the twelve pillars of competitiveness. The observed positive consonances show certain changes and trends that may yield fruitful further analyses by interested economists. The presented approach for InterCriteria Decision Making also presents as a useful application of the theory of index matrices and of intuitionistic fuzzy sets.

The conclusions about how the competitiveness pillars correlate might help answer many questions about how European economies innovate, and would be useful for the EU Member States' national policy makers, in order to better identify and strengthen the transformative forces that drive the future economic growth of their countries. Despite that we have focused on data related to EU Member States, the same approach can be equally applied to other selections of countries and time periods, and analysing the differences with the hitherto presented results will be very informative and challenging.

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